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MOdeling
Nuclear
STructure and
REactions

Parity violating asymmetry and dipole polarizability:
how do they reconcile with each other?

Xavier Roca-Maza

Nuclear Structure and Dynamics - NSD 2024

May 27 - 31, 2024

Valencia, Spain



UNIVERSITAT DE
BARCELONA



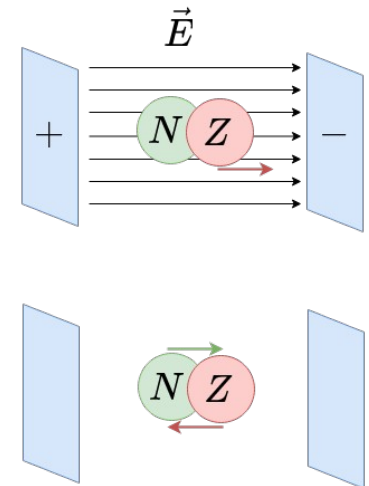
Electric Dipole Polarizability: introduction

The **electric dipole polarizability** measures the **tendency** of the nuclear **charge distribution** to be **distorted**

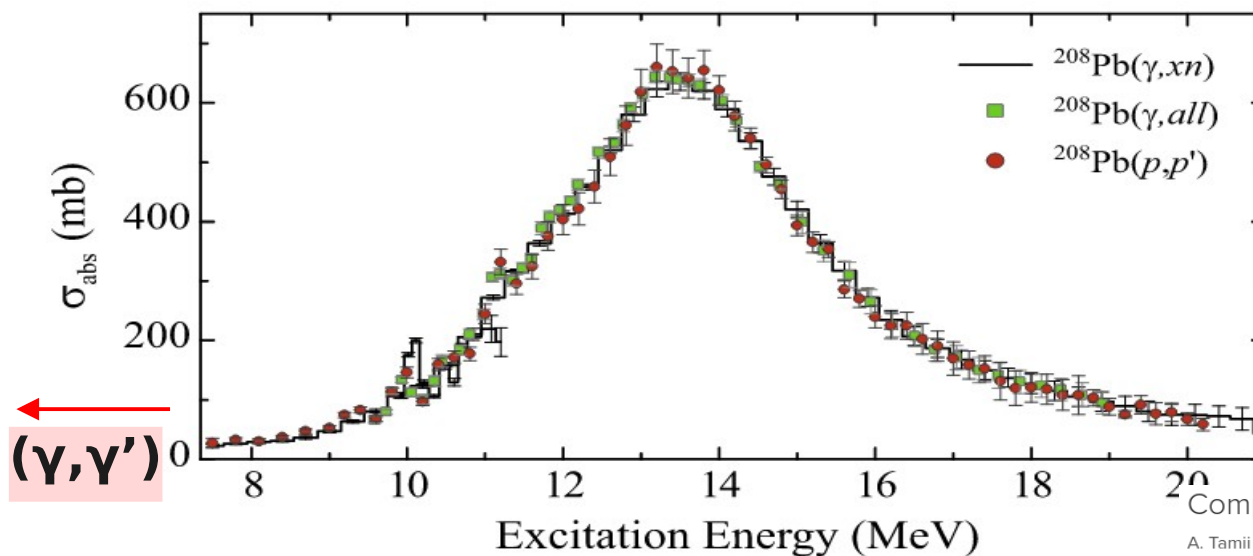
$$\alpha = \frac{\text{electric dipole moment}}{\text{external electric field applied}}$$

Microscopically, it relates with the **photo-absorption cross-section**

$$\alpha_D = \frac{\hbar c}{2\pi^2 e^2} \int \frac{\sigma_{\text{abs}}}{\omega^2} d\omega,$$



Measured using **polarized** proton scattering at **very forward angles** (dominated by **E1** and **M1** well separated)



$$\alpha_D(^{208}\text{Pb}) = 19.6 \pm 0.6 \text{ fm}^3$$

Complete Electric Dipole Response and the Neutron Skin in ^{208}Pb

A. Tamii et al.
Phys. Rev. Lett. **107**, 062502 – Published 3 August 2011

Electric Dipole Polarizability: theory

Theoretically, the total **photo-absorption cross section**, can be written as

$$\sigma_{\gamma-\text{abs}} = 4\pi^2\alpha \sum_{\nu} (E_{\nu} - E_0) |\langle \nu | F_{\text{dipole}} | 0 \rangle|^2$$

Dipole operator
subtract
CM motion

And, thus,

$$\alpha_D = 2 \sum_{\nu \neq 0} \frac{|\langle \nu | F_{\text{dipole}} | 0 \rangle|^2}{E_{\nu} - E_0} \equiv 2m_{-1}$$

$$\frac{eN}{A} \sum_{i=1}^Z r_i Y_{1M}(\hat{r}_i) - \frac{eZ}{A} \sum_{i=1}^N r_i Y_{1M}(\hat{r}_i)$$

Considering the G.S. perturbed by an **external field** λF (with $\lambda \rightarrow 0$). $\langle H \rangle = \langle H_0 + \lambda F_{\text{dipole}} \rangle$ can be written as:

$$\delta \langle \mathcal{H} \rangle = \lambda^2 \sum_{\nu \neq 0} \frac{|\langle \nu | F | 0 \rangle|^2}{E_{\nu} - E_0} + \mathcal{O}(\lambda^3) = \lambda^2 m_{-1} + \mathcal{O}(\lambda^3)$$

$$m_{-1} = \frac{1}{2} \frac{\partial^2 \langle \mathcal{H} \rangle}{\partial \lambda^2} \Big|_{\lambda=0}$$

**Dielectric
Theorem**

Electric Dipole Polarizability: simple model & correlations

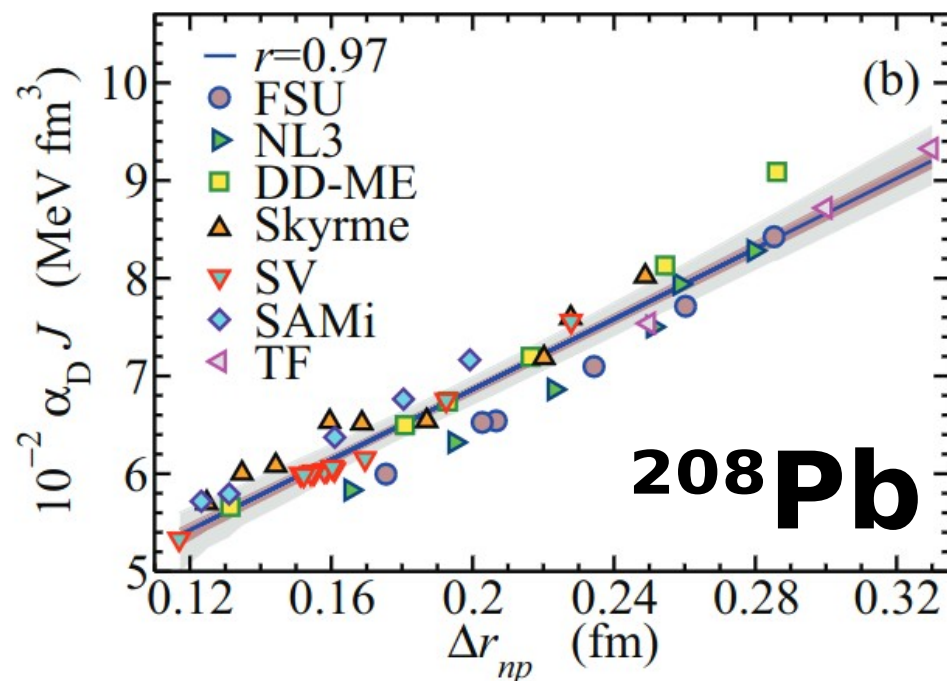
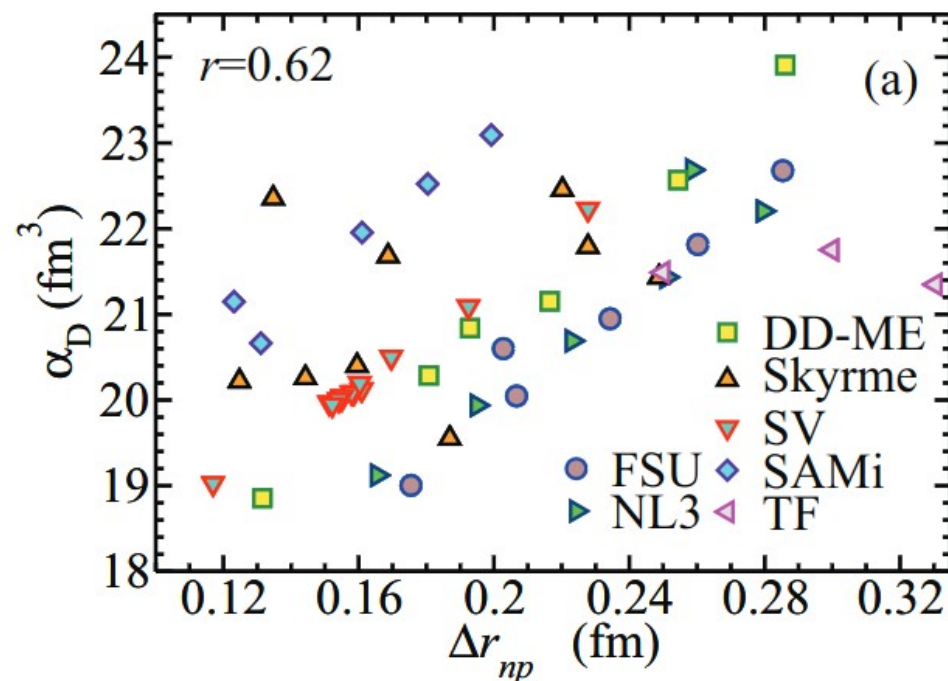
Applying the **dielectric theorem** to the **Droplet Model** Hamiltonian (first Migdal and latter on Meyer et al. NPA385, 269) one can find

$$\alpha_D \approx \frac{A \langle r^2 \rangle}{12J} \left[1 + \frac{5 \Delta r_{np} + \sqrt{\frac{3}{5} \frac{e^2 Z}{70J}} - \Delta r_{np}^{\text{surface}}}{\langle r^2 \rangle^{1/2} (I - I_C)} \right]$$

$J = e(\text{PNM}) - e(\text{SNM}) \rightarrow$
Symmetry energy at ρ_0
 $\Delta r_{np} = \langle r_n^2 \rangle^{1/2} - \langle r_p^2 \rangle^{1/2} \rightarrow$
Neutron skin thickness

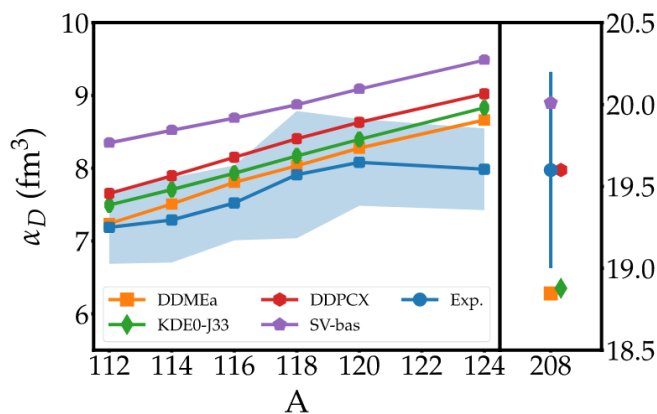
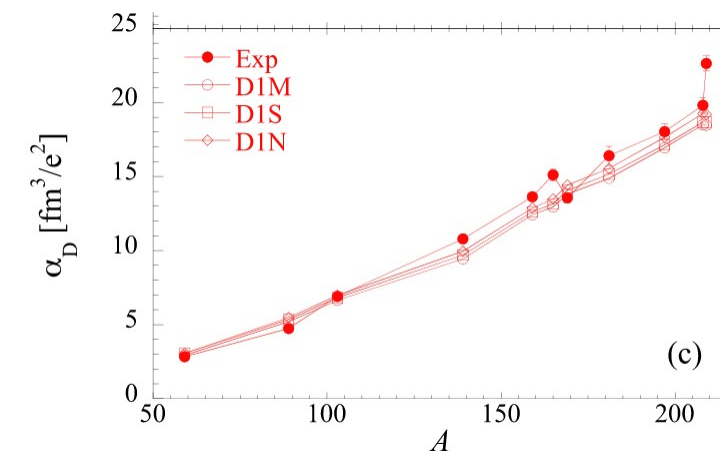
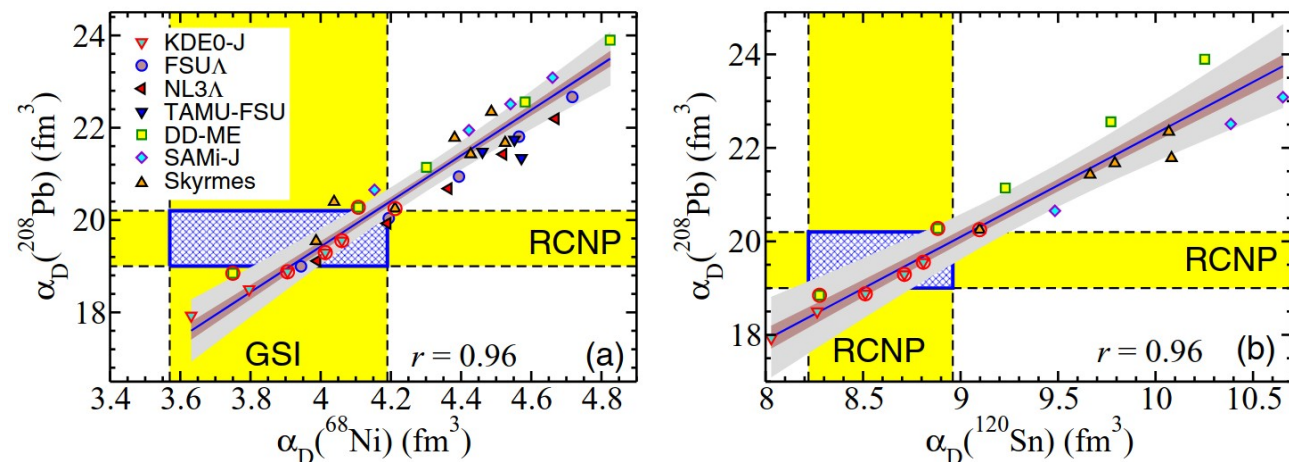
Using microscopic calculations

(Energy Density Functionals $\leftrightarrow$ Hartree-Fock+Random Phase Approximation)

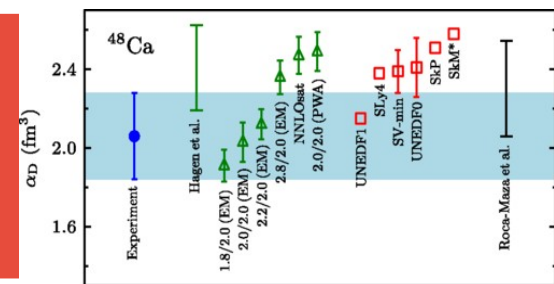


Electric Dipole Polarizability: measurements vs theory

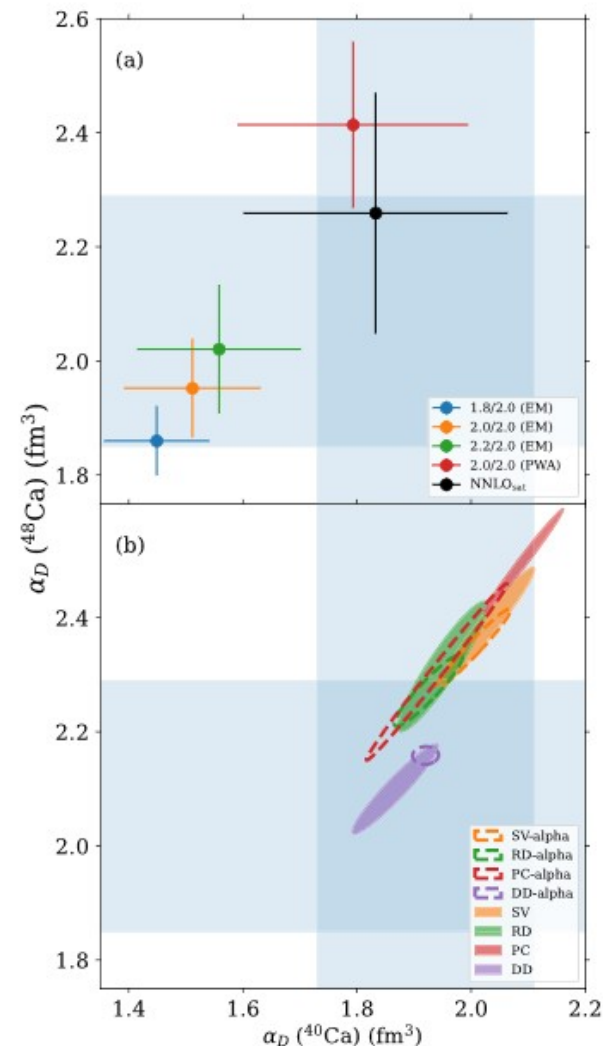
X. Roca-Maza, X. Viñas, M. Centelles, B. K. Agrawal, G. Colò, N. Paar, J. Piekarewicz, and D. Vretenar
Phys. Rev. C **92**, 064304 – Published 8 December 2015



S. Bassauer, P. von Neumann-Cosel, P.-G. Reinhard et al.
Physics Letters B **810** (2020) 135804



J. Birkhan, M. Miorelli, S. Bacca, S. Bassauer, C. A. Bertulani, G. Hagen, H. Matsubara, P. von Neumann-Cosel, T. Papenbrock, N. Pietralla, V. Yu. Ponomarev, A. Richter, A. Schwenk, and A. Tamii
Phys. Rev. Lett. **118**, 252501 – Published 23 June 2017



S. Goriely, S. Péru, G. Colò, X. Roca-Maza, I. Gheorghe, D. Filipescu, and H. Utsunomiya
Phys. Rev. C **102**, 064309 – Published 9 December 2020

R. W. Fearick, P. von Neumann-Cosel, S. Bacca, J. Birkhan, F. Bonaiti, I. Brandherm, G. Hagen, H. Matsubara, W. Nazarewicz, N. Pietralla, V. Yu. Ponomarev, P.-G. Reinhard, X. Roca-Maza, A. Richter, A. Schwenk, J. Simonis, and A. Tamii
Phys. Rev. Research **5**, L022044 – Published 31 May 2023

Parity Violating Asymmetry: introduction

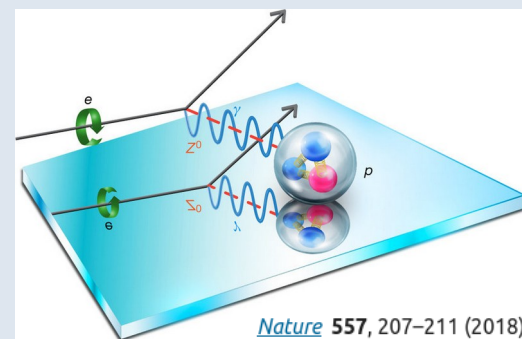
Elastic electron scattering by nuclei:

→ **Parity conserving**

Exchange of γ that essentially couples to protons $Q_p^c=1$; $Q_n^c=0$

→ **Parity violating**

Exchange Z^0 that essentially couples to neutrons $Q_p^w=0.07$; $Q_n^w=-0.99$



Ultra-relativistic electrons ($m_e \rightarrow 0$) **aligned** (+) or **anti-aligned** (-) to the beam line, in approaching the nucleus:

$$[\vec{\alpha} \cdot \vec{p} + V_{\text{Coulomb}}(\vec{r}) \pm V_{\text{Weak}}(\vec{r})] \Psi_{\pm} = E \Psi_{\pm}$$

$$\sigma \approx \left| \text{Diagram 1} + \text{Diagram 2} \right|^2$$

Diagram 1: Electron (e^-) interacting with a nucleus (^{208}Pb) via a photon (γ).

Diagram 2: Electron (e^-) interacting with a nucleus (^{208}Pb) via a Z^0 boson.

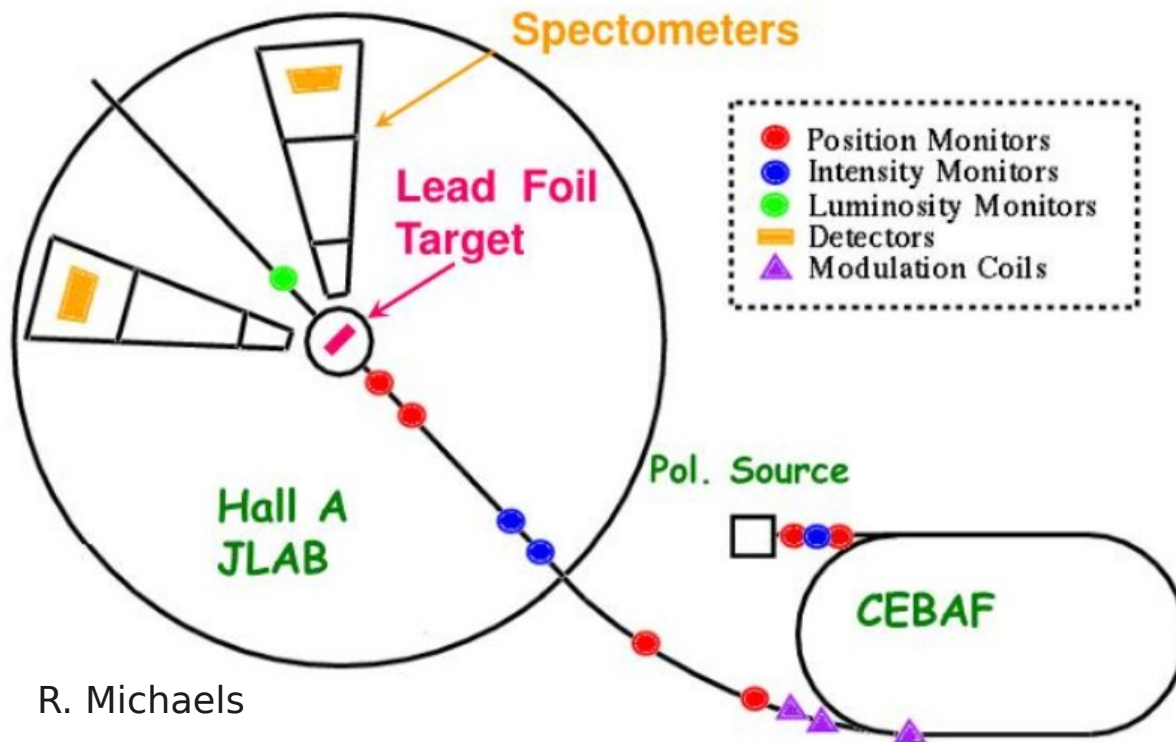
One can get **advantage** from this **interference pattern** between **electromag.** and **weak** interact.

$$A_{PV} = \frac{\frac{d\sigma_+}{d\Omega} - \frac{d\sigma_-}{d\Omega}}{\frac{d\sigma_+}{d\Omega} + \frac{d\sigma_-}{d\Omega}} \approx \frac{\text{Weak}}{\text{Coulomb}}$$

Parity Violating Asymmetry: experiment

Lead and Calcium Radius Experiments PREx & CREx @ JLab

$$A_{PV} \sim \frac{G_F}{4\sqrt{2}\pi\alpha} Q^2 \sim 10^{-4} (Q[\text{GeV}])^2$$



→ Spectrometers $\sim 5^\circ$

→ e^- beam $E \sim \text{GeV}$

$$Q_{\text{PREx}}^2 = 0.00616 \text{ GeV}^2$$

$$Q_{\text{CREx}}^2 = 0.0297 \text{ GeV}^2$$

→ Demanding experiment:

For **10^6 electrons** or more
only **one** of them **interact weakly** with the nucleus

**Proposed new experiment
on ^{208}Pb @ Mainz !!!**

Parity Violating Asymmetry: theory

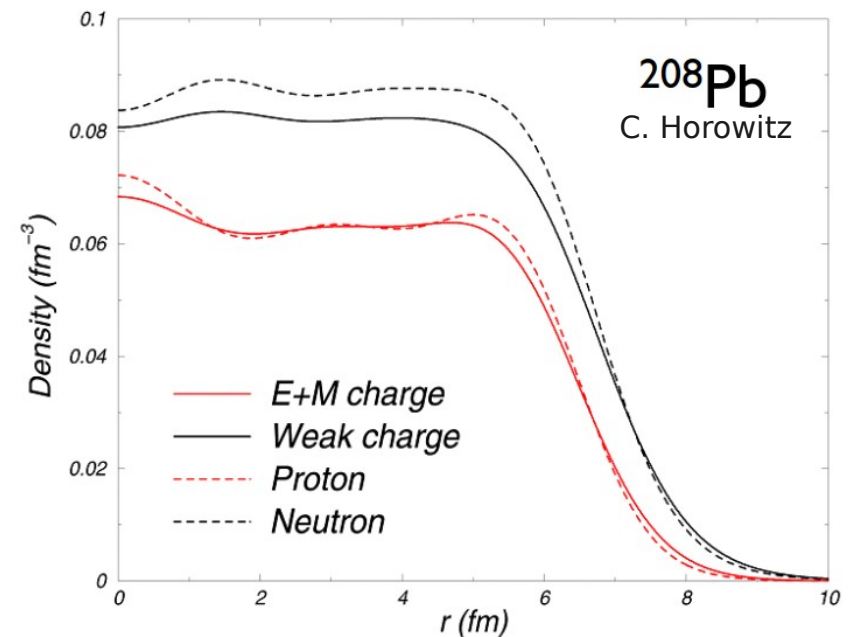
To solve the **Dirac equation**

$$[\vec{\alpha} \cdot \vec{p} + V_{\text{Coulomb}}(\vec{r}) \pm V_{\text{Weak}}(\vec{r})] \Psi_{\pm} = E \Psi_{\pm}$$

The main inputs are the **electromagnetic** ρ_{ch} and **weak charge** ρ_{W} distributions

$$V_{\text{Coulomb}}(\vec{r}) = Z\alpha \int \frac{\rho_{\text{ch}}(\vec{r}')}{|\vec{r} - \vec{r}'|} d\vec{r}' \quad V_{\text{Weak}}(\vec{r}) = \frac{G_F}{2\sqrt{2}} \rho_{\text{W}}(\vec{r})$$

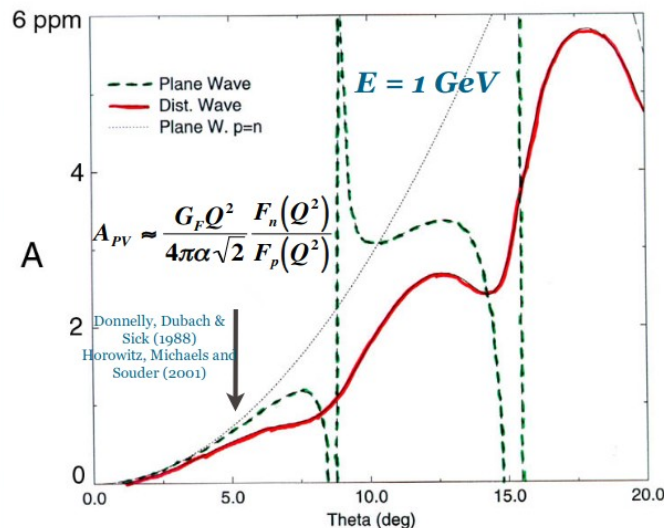
We need to know the **neutron and proton distributions** in nuclei and the **electromagnetic and weak charge form factors** of the **neutron** and the **proton**



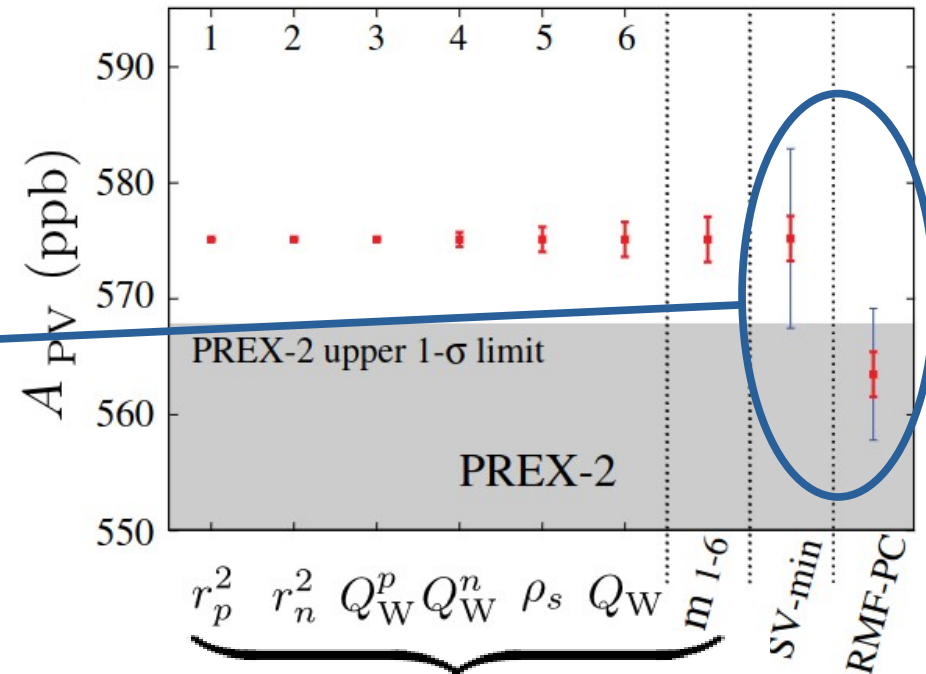
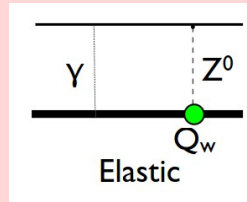
Parity Violating Asimmetry: theory

The **main uncertainties** come from **nuclear model errors** on the description of the **neutron distribution (blue error bars)**

→ **Coulomb distortions are important** (order αZ)



Are γZ^0 box corrections **important?** not included



Hadronic uncertainties less relevant

Parameter	Value
$\langle r_p^2 \rangle \text{ (fm}^2\text{)}$	0.726 ± 0.019
$\langle r_n^2 \rangle \text{ (fm}^2\text{)}$	-0.1161 ± 0.0022
μ_p	$2.792\,847$
μ_n	-1.9130
$Q_p^{(W)}$	0.0713 ± 0.0001
$Q_n^{(W)}$	-0.9888 ± 0.0011
ρ_s	-0.24 ± 0.70
κ_s	-0.017 ± 0.004
$Q_{126.82}^{(W)}$	-117.9 ± 0.3

Parity Violating Asimmetry: simple model & correlations

The **parity violating asymmetry** within the **PWBA**:

$$A_{PV}^{PWBA} = \frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \left[\underbrace{4\sin^2 \theta_W}_{\approx 1} + \frac{F_n(Q) - F_p(Q)}{F_p(Q)} \right]$$

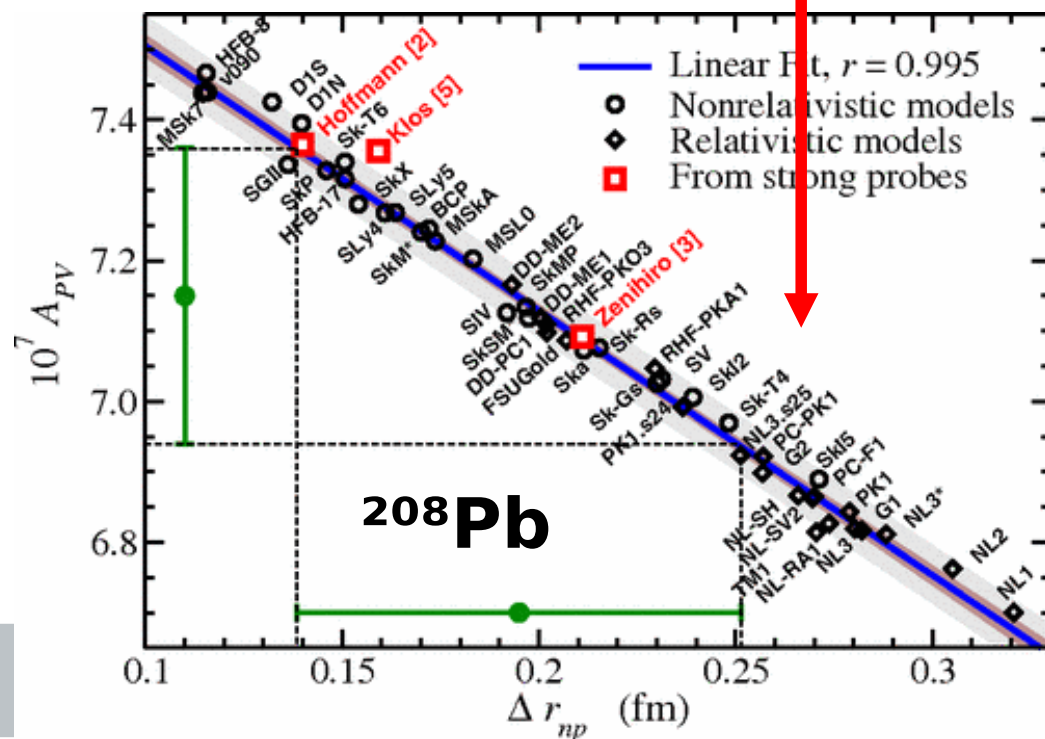
$$\xrightarrow{Q \rightarrow 0} \frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \left[1 - \frac{Q^2 \langle r_p^2 \rangle}{3} \frac{\Delta r_{np}}{\langle r_p^2 \rangle^{1/2}} \right]$$

30% error (for PREx) due to Coulomb distortions does not blur **the main physics**

The **parity violating asymmetry** within the **DWBA**:

○◇ → Energy Density Functionals

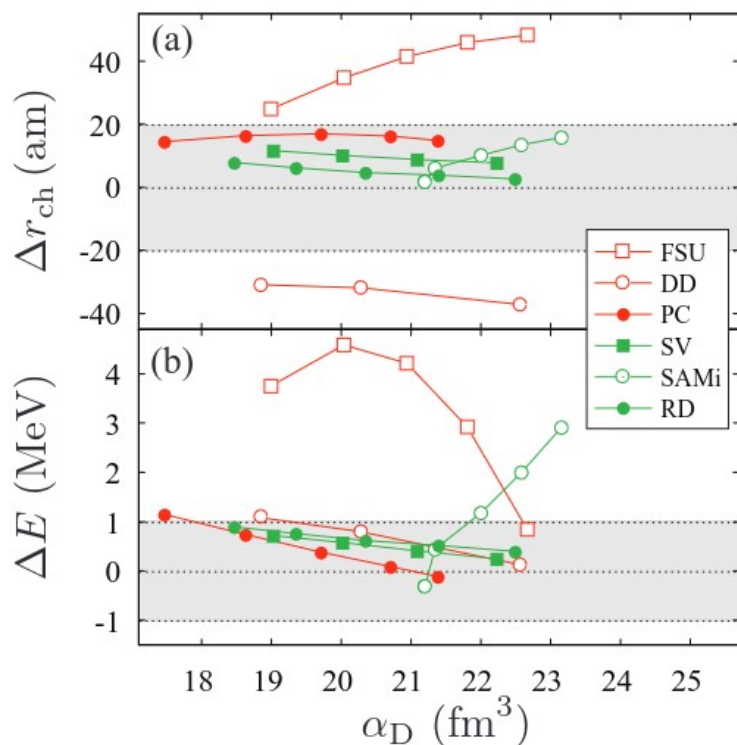
◻ → Experimental ρ_n from hadronic probes + ρ_p from e^- scattering



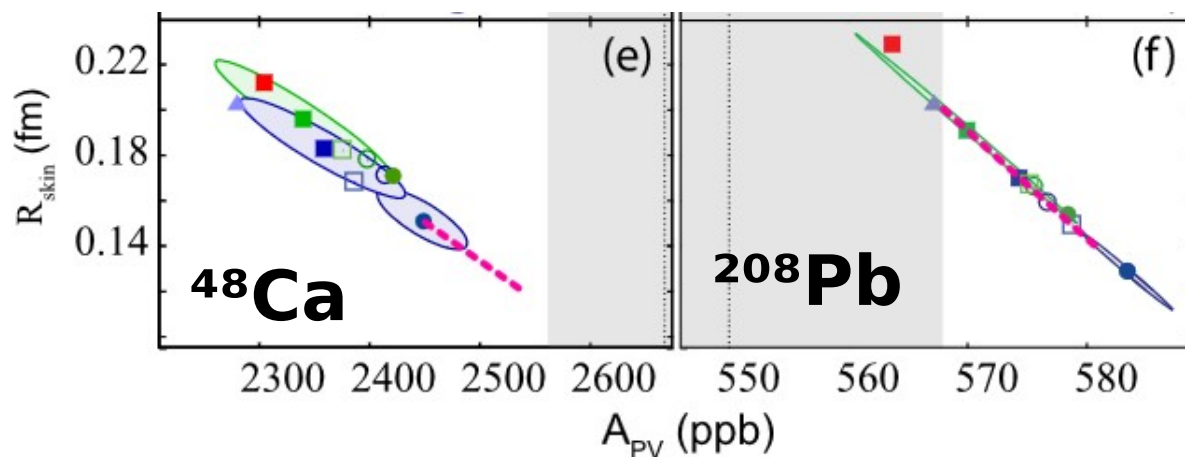
Parity Violating Asymmetry: measurements vs. theory

Selecting those models we consider **well calibrated** to masses and radii

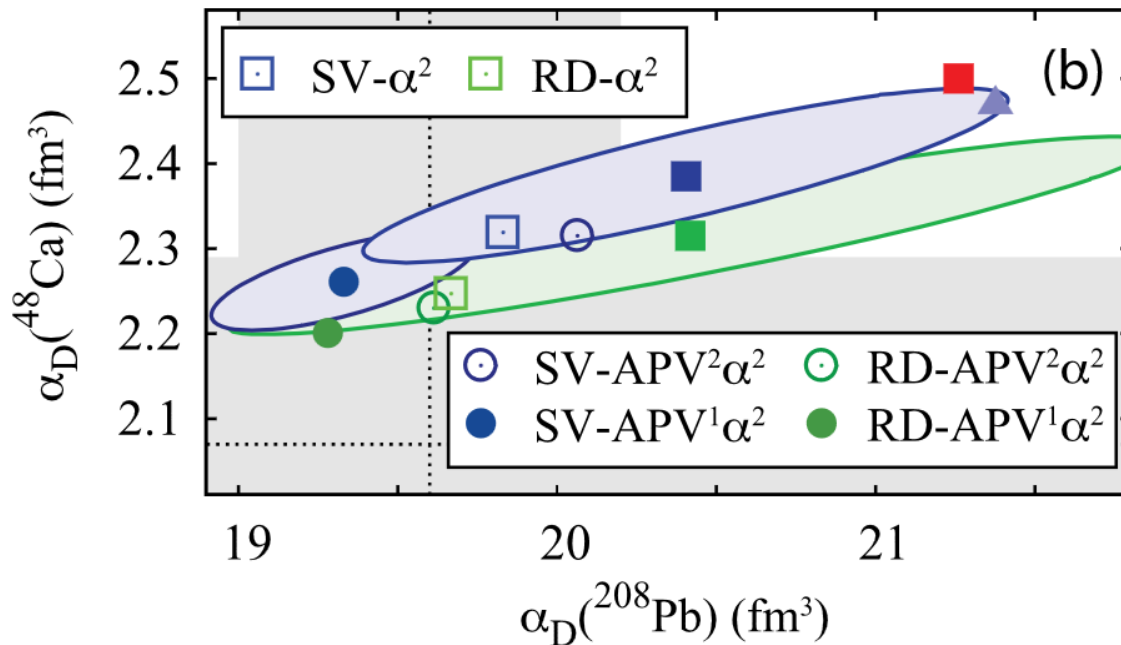
Theoretical (**EDFs** and **ab initio**) and experimental 1σ errors overlap in ^{208}Pb but not in ^{48}Ca → **No simultaneous description**



Fitting protocol also including A_{PV} and α_D



Summary: model performance A_{PV} (sensitive to Δr_{np}) and α_D (sensitive to J and Δr_{np}) in ^{48}Ca and ^{208}Pb



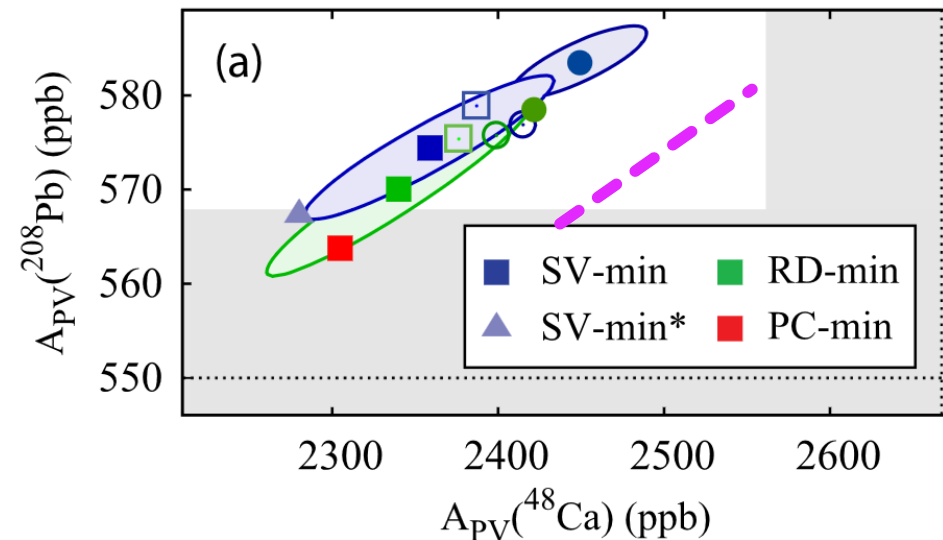
No simultaneous description of **parity violating asymmetries** (ground state observable) → point to a **deficient understanding** of **neutron skins**

Simultaneous description of **dipole polarizabilities** → point to a **good understanding** of **symmetry energy (J)** and **neutron skins (Δr_{np})**

Ab-initio (B. Hu) Nature Physics (2022)

$$\alpha_D(^{48}\text{Ca}) \quad 2.30^{+0.31}_{-0.26}$$

$$\alpha_D(^{208}\text{Pb}) \quad 22.6^{+2.1}_{-1.8}$$



How do A_{PV} and α_D reconcile with each other?

Different ways to learn about the **neutron distribution** in atomic nuclei using **different observables** provide **different answers**



However, within **1.5σ** all looks fine, both from phenomenologic **Energy Density Functionals** and from **Ab Initio**

From Theory:

- An effort to better understand the **parity violating asymmetry** and the **beam normal spin asymmetry** in ^{208}Pb is needed.
- An effort to better understand the **systematics** on the **dipole polarizability** is needed (e.g. along the Sn isotopic chain; ^{209}Bi ?).

From Experiment:

- An effort to improve the accuracy in the **parity violating asymmetry** in ^{208}Pb (and/or measure other Q values) and to confirm the measured values for the **beam normal spin asymmetry** is needed
- **Systematic** measurements of the **dipole polarizability** along **neutron rich** isotopic chains (such as for $N > 74$ Sn isotopes)

Collaborators

- Gianluca **Colò** (University of Milan)
- Hiroyuki **Sagawa** (University of Aizu & RIKEN)
- Tomoya **Naito** (University of Tokyo & RIKEN)
- Shihang **Shen** (Forschungszentrum Jülich)
- Xavier **Vinyes** & Mario **Centelles** (University of Barcelona)
- Jorge **Piekarewicz** (Florida State University)
- Nils **Paar** & Dario **Vretenar** (University of Zagreb)
- Bijay K. **Agrawal** (Saha Institute of Nuclear Physics)
- P.-G. **Reinhard** (University of Erlangen-Nürnberg)
- Witold **Nazarewicz** (FRIB and Michigan State University)