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The neutron skin thickness in atomic nuclei

Xavier Roca-Maza

U. Barcelona & U. Milan

August 19th de 2026
University of Jyväskylä

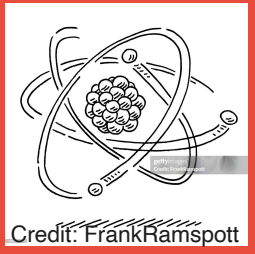


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Neutron skin thickness in atomic nuclei

What is it?



The **mean square radius** of the **neutron** (n) or **proton** (p) **density distribution** ($\rho_q(\vec{r})$ with $q = n, p$) is defined as:

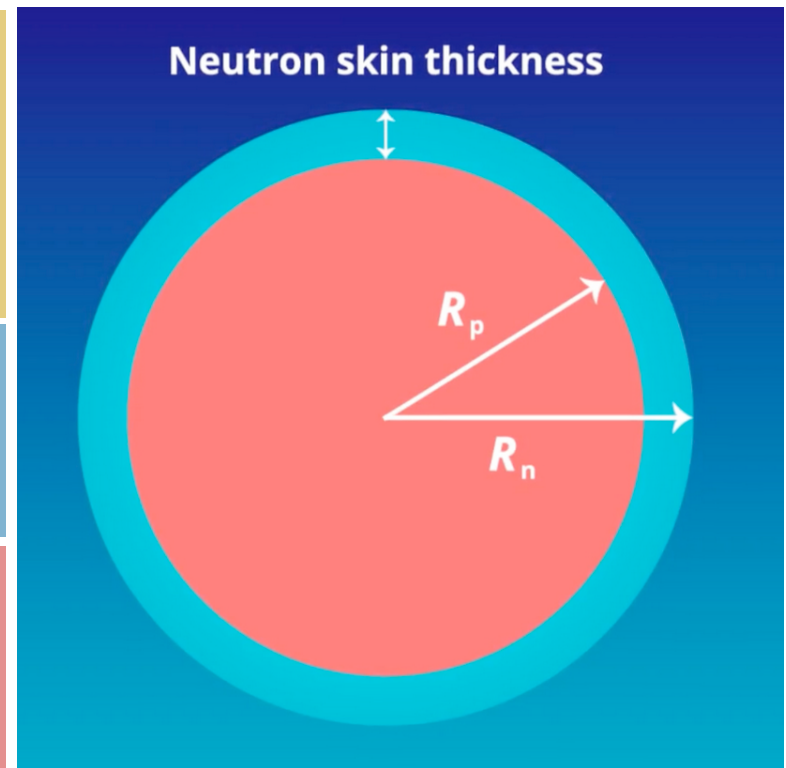
$$\langle r_q^2 \rangle = \int d\vec{r} r^2 \rho_q(\vec{r})$$

The neutron skin thickness is defined as the difference between the neutron and proton radii

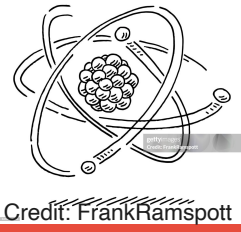
$$\Delta r_{np} \equiv \langle r_n^2 \rangle^{1/2} - \langle r_p^2 \rangle^{1/2}$$

For **atomic nuclei** with $N > Z$ we expect a **neutron skin**, **larger** as **larger the** average repulsion (**pressure**) felt by the neutrons

In **first approximation** (within a Local Density Approximation) **the pressure** that a **neutron uniform system feels** at the densities typical for the atomic nucleus



An important physical insight!

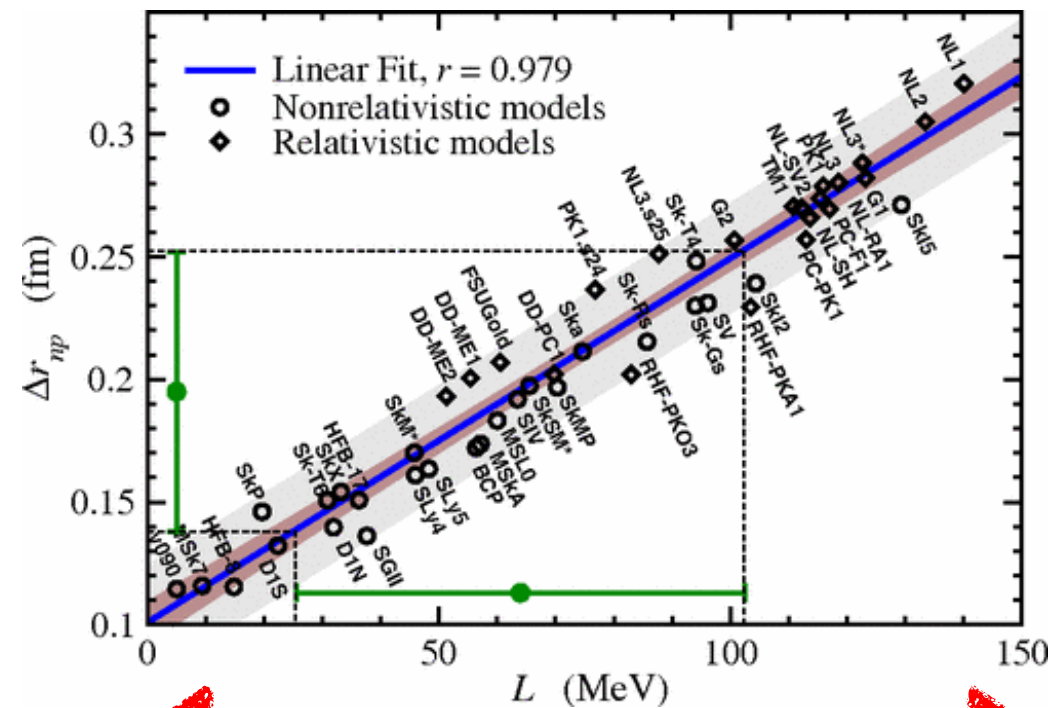
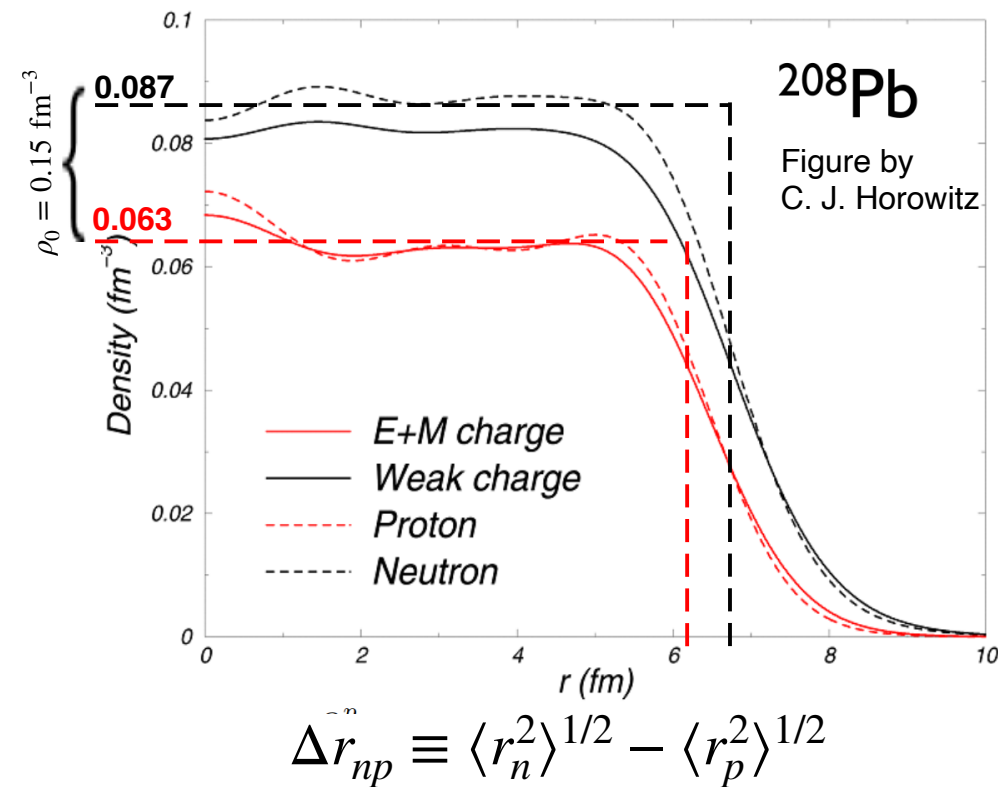


Neutron skin thickness is a **proxy** to the pressure (**nuclear force**) of an **ideal uniform system** composed only by neutrons and protons (L)

Droplet Model:

$$\Delta r_{np} \approx \frac{1}{12} \frac{N - Z}{A} \frac{R}{J} L$$

State-of-the-art microscopic models:



Model predictions are very spread

Neutron skin thickness in atomic nuclei

Why is it important?

Constraints the nuclear equation of state (EoS)

The neutron skin is strongly linked to the density dependence of the energy per particle in a uniform system

[WE WILL DISCUSS THIS IN WHAT FOLLOWS]

Connects nuclei to neutron stars

The same physics governing neutron skins also determines properties of neutron stars related to their size and deformability (quadruple polarizability) as well as how exotic are nuclei present in their crusts.

Tests nuclear structure models

Precise measurements discriminate between competing theoretical models, improving our understanding of nuclear forces.

Impacts reactions and stability of exotic nuclei

Neutron distribution affects reaction cross sections, decay properties, and predictions for very neutron-rich nuclei (relevant for rare-isotope physics).

Informs r-process nucleosynthesis

Better constraints on neutron-rich matter improve models of heavy element formation in astrophysical environments.

Provides electroweak physics tests

Techniques like parity-violating electron scattering probe neutron distributions with minimal strong-interaction uncertainties, offering clean tests of the Standard Model in nuclei.

Nuclear Equation of State (EoS)

What is it? How is defined?

Definition: the **energy** (E) per **nucleon** ($A=N+Z$), $e \equiv E/A$, of an **uniform system of neutrons** (N) and **protons** (Z) as a function of the **neutron** ($\rho_n = N/V$) and **proton** ($\rho_p = Z/V$) **densities** ...

→ ... **at zero temperature:** room temperature $10^2\text{K} \rightarrow 10^{-8}$ MeV while “cold” neutron stars are at about $10^{10}\text{K} \rightarrow 1$ MeV. **Separation energy** in stable nuclei (equivalent to ionization energy in atoms) is of several MeV.

→ ... **unpolarized:** energy favors **couples** of neutrons and protons **occupying the same state but with opposite spins** (equivalent to electrons in atoms)

→ ... **isospin symmetric:** neutron-neutron, proton-proton and neutron-proton **nuclear interaction** are very **similar** among them. **Masses** of neutrons and protons are almost **degenerate**. Hence neutrons and protons can be thought as **two states** of the **same particle** with different isobaric spin or **isospin** (in analogy with spin): the **nucleon**.

→ ... and **no Coulomb:** **idealized uniform system** (focus on strong interaction, much stronger than Coulomb at nuclear scale $\sim 10^{15}$ fm). Real systems are finite and electrically neutral so no divergences in adding Coulomb.

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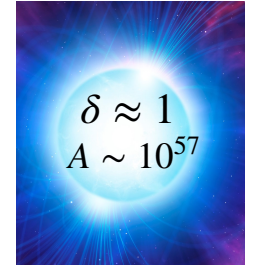
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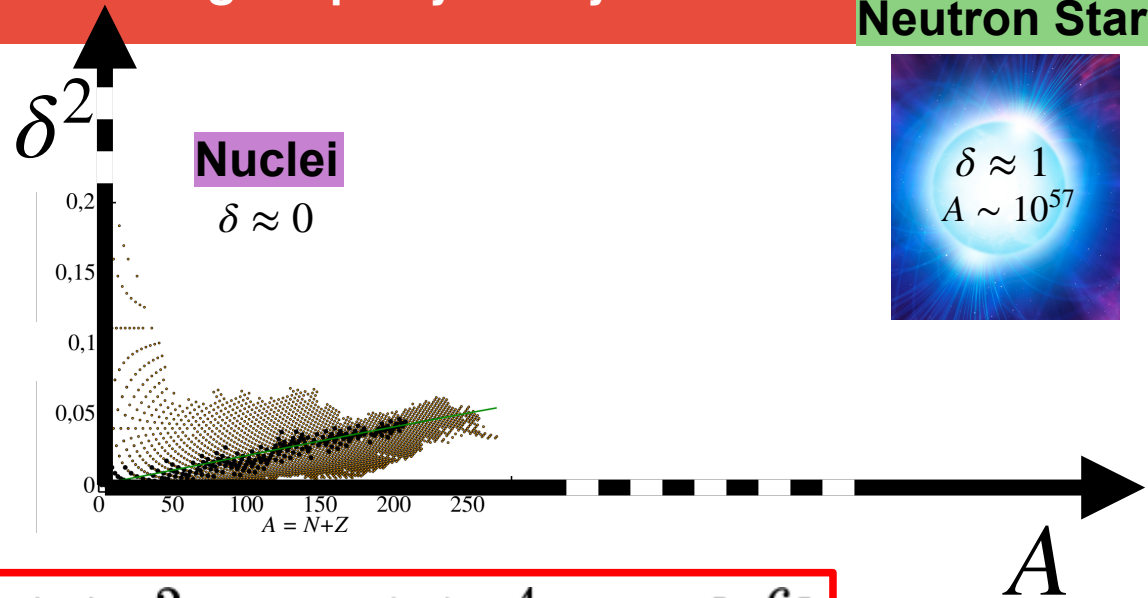
Nuclear Equation of State (EoS)

Unpolarized, uniform nuclear matter at $T=0$ assuming isospin symmetry

Neutron Star

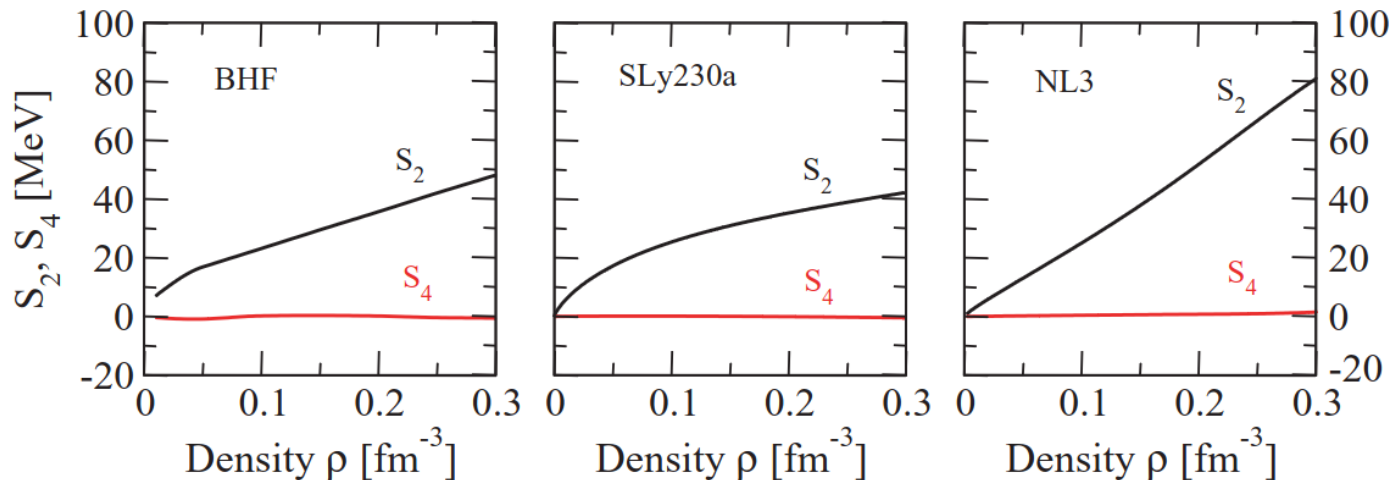


It is convenient to write the energy per nucleon (e) as a function of the total density $\rho = \rho_n + \rho_p$ and the relative difference $\delta = (\rho_n - \rho_p) / \rho$ for $\delta \rightarrow 0$:



A

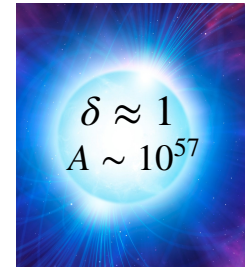
$$e(\rho, \delta) = e(\rho, 0) + S_2(\rho)\delta^2 + S_4(\rho)\delta^4 + \mathcal{O}[\delta^6]$$



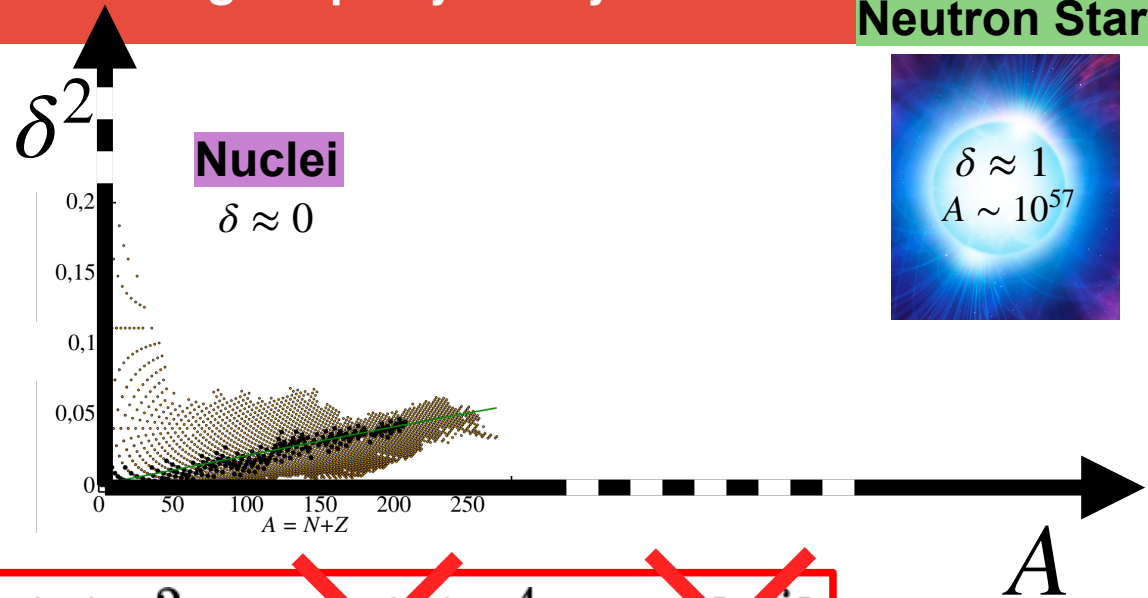
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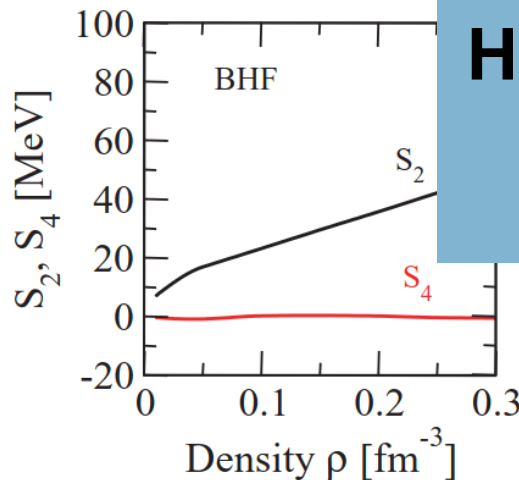


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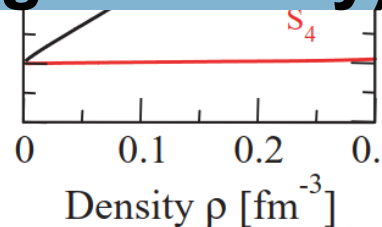
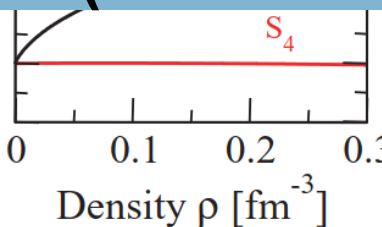


A

$$e(\rho, \delta) = e(\rho, 0) + S_2(\rho)\delta^2 + S_4(\rho)\delta^4 + \mathcal{O}[\delta^6]$$



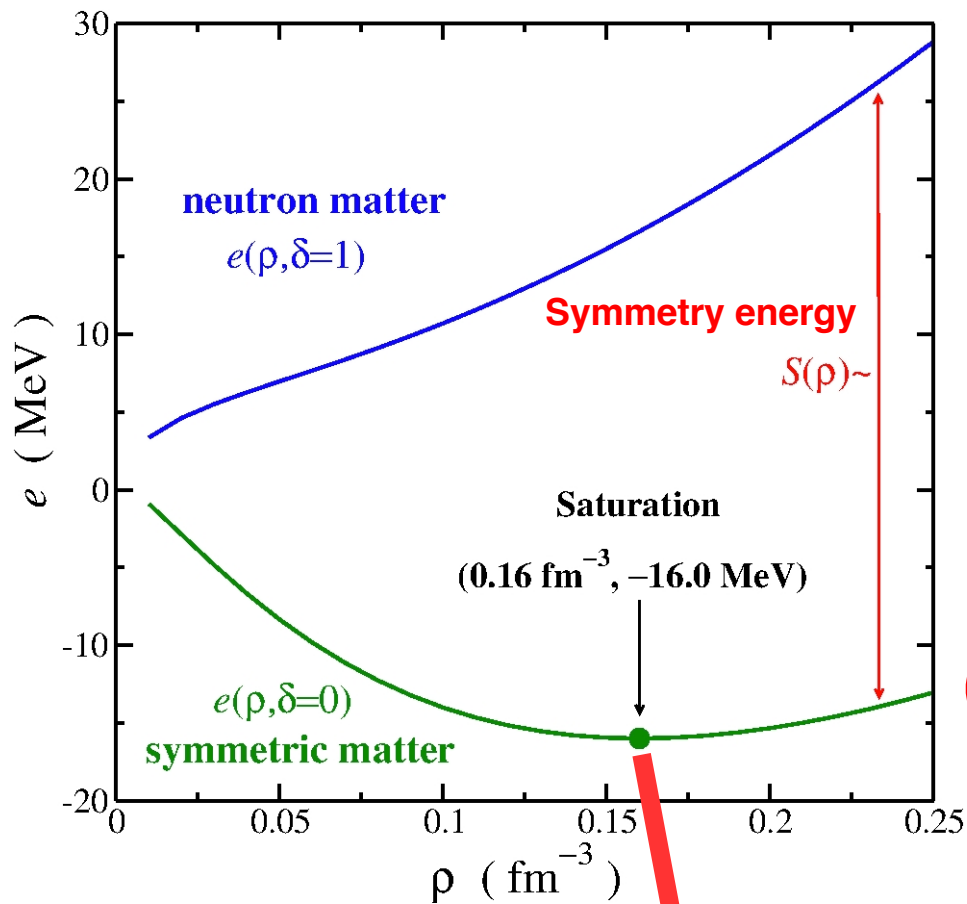
Higher order terms beyond δ^2 do not actually contribute (according to theory)



Nuclear Equation of State (EoS)

Unpolarized, uniform nuclear matter at $T=0$ assuming isospin symmetry

$$e(\rho, \delta) = e(\rho, 0) + S_2(\rho)\delta^2$$



It is customary to **Taylor expand** $e(\rho, 0)$ and $S(\rho)$ around **nuclear saturation density** $\rho_0 \sim 0.16 \text{ fm}^{-3}$

$$e(\rho, 0) = e(\rho_0, 0) + \frac{1}{2}K_0x^2 + \mathcal{O}[\rho^3] \text{ where } x = \frac{\rho - \rho_0}{3\rho_0}$$

$$S(\rho) = J + Lx + \frac{1}{2}K_{\text{sym}}x^2 + \mathcal{O}[\rho^3, \delta^4]$$

K $\rightarrow$ how **compressible** is matter @ ρ_0

J $\rightarrow$ **penalty energy** for systems with $\rho_n \neq \rho_p$ @ $\rho_n + \rho_p = \rho_0$

L $\rightarrow$ **pressure** for systems with $\rho_n \neq \rho_p$ @ ρ_0

$$P = - \left. \frac{\partial E}{\partial V} \right|_{A=\text{const.}} = \frac{1}{3}\rho\delta^2L(\rho)$$

$$P(\rho = \rho_0, \delta = 0) = 0 \text{ MeV fm}^{-3}$$

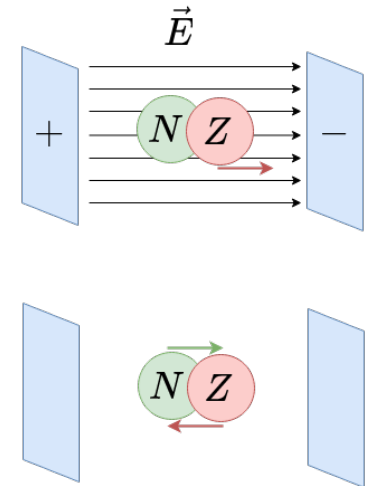
Electric Dipole Polarizability: introduction

The **electric dipole polarizability** measures the **tendency** of the nuclear **charge distribution** to be **distorted**

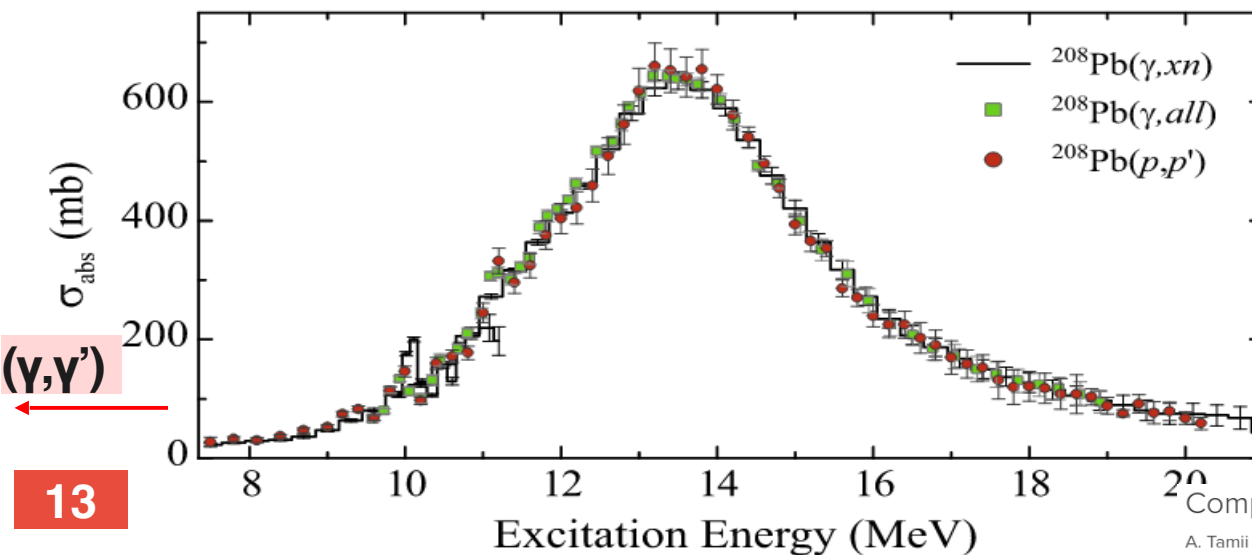
$$\alpha = \frac{\text{electric dipole moment}}{\text{external electric field applied}}$$

Microscopically, it relates with the photo-absorption cross-section

$$\alpha_D = \frac{\hbar c}{2\pi^2 e^2} \int \frac{\sigma_{\text{abs}}}{\omega^2} d\omega,$$



Measured using **polarized** proton scattering at **very forward angles** (dominated by **E1** and **M1** well separated)



$$\alpha_D(^{208}\text{Pb}) = 19.6 \pm 0.6 \text{ fm}^3$$

$$\Delta r_{\text{np}} = 0.156^{+0.025}_{-0.021} \text{ fm}$$

Complete Electric Dipole Response and the Neutron Skin in ^{208}Pb

A. Tamii *et al.*
Phys. Rev. Lett. **107**, 062502 – Published 3 August 2011

Electric Dipole Polarizability: theory

Theoretically, the total **photo-absorption cross section**, can be written as

$$\sigma_{\gamma-\text{abs}} = 4\pi^2\alpha \sum_{\nu} (E_{\nu} - E_0) |\langle \nu | F_{\text{dipole}} | 0 \rangle|^2$$

Dipole
operator
subtract CM
motion

And, thus,

$$\alpha_D = 2 \sum_{\nu \neq 0} \frac{|\langle \nu | F_{\text{dipole}} | 0 \rangle|^2}{E_{\nu} - E_0} \equiv 2m_{-1}$$

$$\frac{eN}{A} \sum_{i=1}^Z r_i Y_{1M}(\hat{r}_i) - \frac{eZ}{A} \sum_{i=1}^N r_i Y_{1M}(\hat{r}_i)$$

Considering the G.S. perturbed by an **external field** λF (with $\lambda \rightarrow 0$):

$\langle \mathcal{H} \rangle = \langle \mathcal{H}_0 + \lambda F_{\text{dipole}} \rangle$; The variation in the expectation energy can be written as:

$$\delta \langle \mathcal{H} \rangle = \lambda^2 \sum_{\nu \neq 0} \frac{|\langle \nu | F | 0 \rangle|^2}{E_{\nu} - E_0} + \mathcal{O}(\lambda^3) = \lambda^2 m_{-1} + \mathcal{O}(\lambda^3)$$

$$m_{-1} = \frac{1}{2} \frac{\partial^2 \langle \mathcal{H} \rangle}{\partial \lambda^2} \Big|_{\lambda=0}$$

**Dielectric
Theorem**

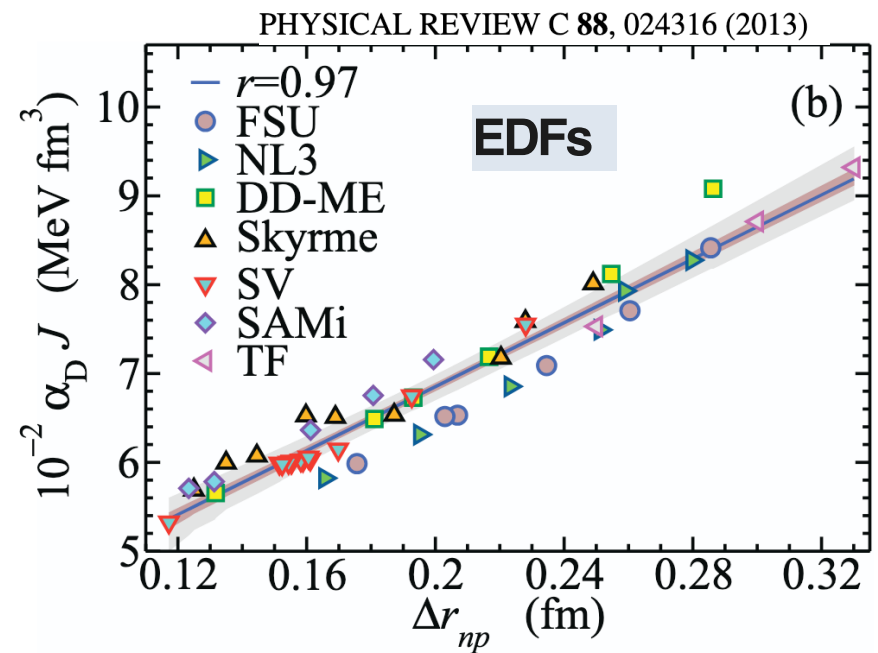
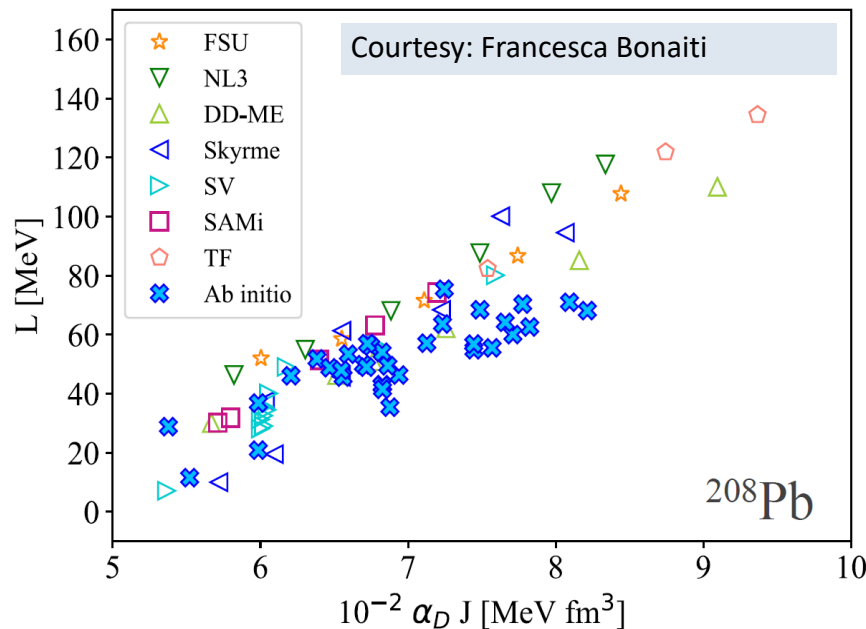
Electric Dipole Polarizability: simple model & correlations

Applying the **dielectric theorem** to the **Droplet Model** Hamiltonian (first Migdal and latter on Meyer et al. NPA385, 269) one can find

$$\alpha_D \approx \frac{A \langle r^2 \rangle}{12J} \left[1 + \frac{5 \Delta r_{np} + \sqrt{\frac{3}{5} \frac{e^2 Z}{70J}} - \Delta r_{np}^{\text{surface}}}{\langle r^2 \rangle^{1/2} (I - I_C)} \right]$$

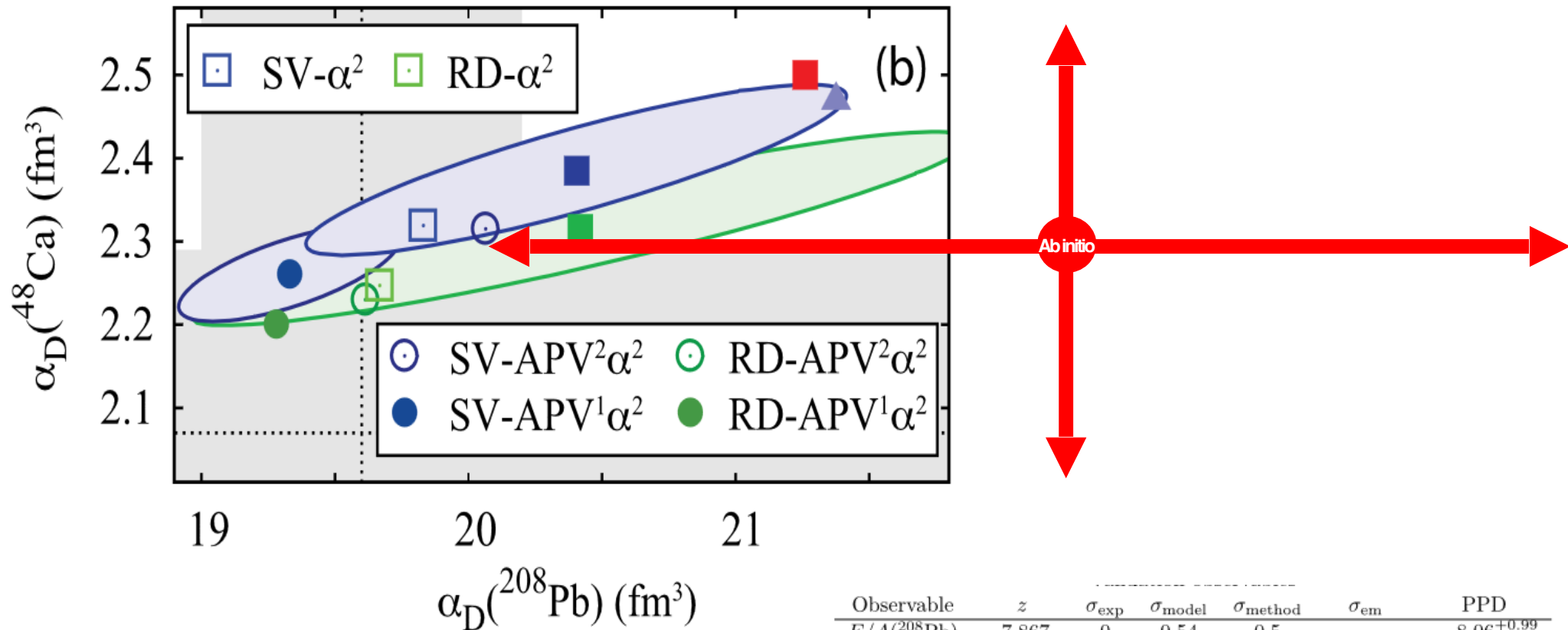
$J = e(\text{PNM}) - e(\text{SNM}) \rightarrow$ Symmetry energy at ρ_0
 $\Delta r_{np} \equiv \langle r_n^2 \rangle^{1/2} - \langle r_p^2 \rangle^{1/2} \rightarrow$ Neutron skin thickness

Using microscopic calculations (Energy Density Functionals & Ab initio)



$$\alpha_D J = (301 \pm 32) + (1922 \pm 73) \Delta r_{np}$$

Electric Dipole Polarizability in ^{48}Ca and ^{208}Pb



Combined Theoretical Analysis of the Parity-Violating Asymmetry for ^{48}Ca and ^{208}Pb

Paul-Gerhard Reinhard, Xavier Roca-Maza, and Witold Nazarewicz
Phys. Rev. Lett. **129**, 232501 – Published 2 December 2022

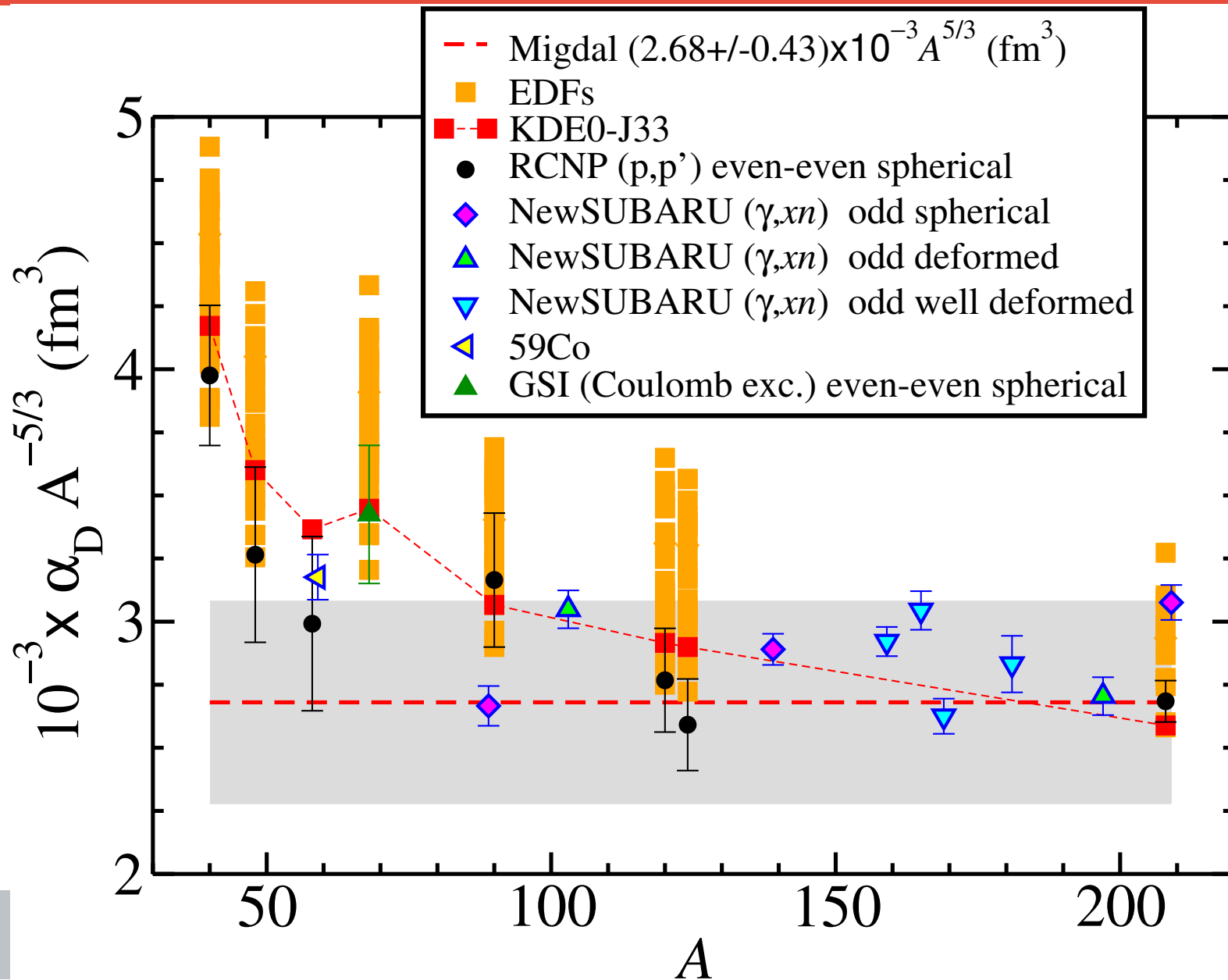
Observable	z	σ_{exp}	σ_{model}	σ_{method}	σ_{em}	PPD
$E/A(^{208}\text{Pb})$	-7.867	0	0.54	0.5	—	$-8.06^{+0.99}_{-0.88}$
$R_p(^{208}\text{Pb})$	5.45	0	0.17	0.05	—	$5.43^{+0.21}_{-0.23}$
$\alpha_D(^{48}\text{Ca})$	2.07	0.22	0.06	0.1	—	$2.30^{+0.31}_{-0.26}$
$\alpha_D(^{208}\text{Pb})$	20.1	0.6	0.59	0.8	—	$22.6^{+2.1}_{-1.8}$

Ab initio predictions link the neutron skin of ^{208}Pb to nuclear forces

Baishan Hu, Weiguang Jiang, Takayuki Miyagi, Zhonghao Sun, Andreas Ekström, Christian Forssén, Gaute Hagen, Jason D. Holt, Thomas Papenbrock, S. Ragnar Stroberg & Ian Vernon

Nature Physics **18**, 1196–1200 (2022) | [Cite this article](#)

Electric Dipole Polarizability: How nuclear models perform for other nuclei?



Parity Violating Asymmetry: introduction

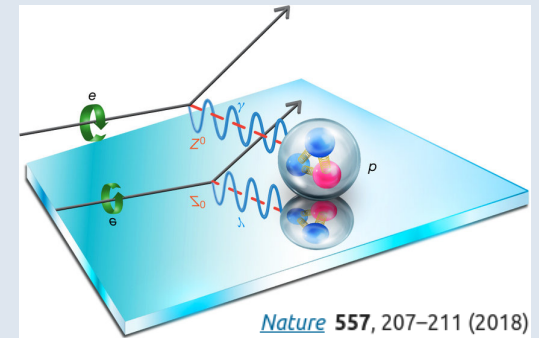
Elastic electron scattering by nuclei:

→ **Parity conserving**

Exchange of γ that essentially couples to protons $Q_p^c=1$; $Q_n^c=0$

→ **Parity violating**

Exchange Z_0 that essentially couples to neutrons $Q_p^w=0.07$; $Q_n^w=-0.99$



Ultra-relativistic electrons ($m_e \rightarrow 0$) with spin **aligned** (+) or **anti-aligned** (-) to the beam line, in approaching the nucleus:

$$[\vec{\alpha} \cdot \vec{p} + V_{\text{Coulomb}}(\vec{r}) \pm V_{\text{Weak}}(\vec{r})] \Psi_{\pm} = E \Psi_{\pm}$$

$$\sigma \approx \left| \text{Diagram 1} + \text{Diagram 2} \right|^2$$

Diagram 1: Electron (e^-) interacting with a nucleus (^{208}Pb) via a photon (γ).

Diagram 2: Electron (e^-) interacting with a nucleus (^{208}Pb) via a Z^0 boson.

One can get **advantage** from this **interference pattern** between **electromag.** and **weak** interact.

$$A_{PV} = \frac{\frac{d\sigma_+}{d\Omega} - \frac{d\sigma_-}{d\Omega}}{\frac{d\sigma_+}{d\Omega} + \frac{d\sigma_-}{d\Omega}} \approx \frac{\text{Weak}}{\text{Coulomb}}$$

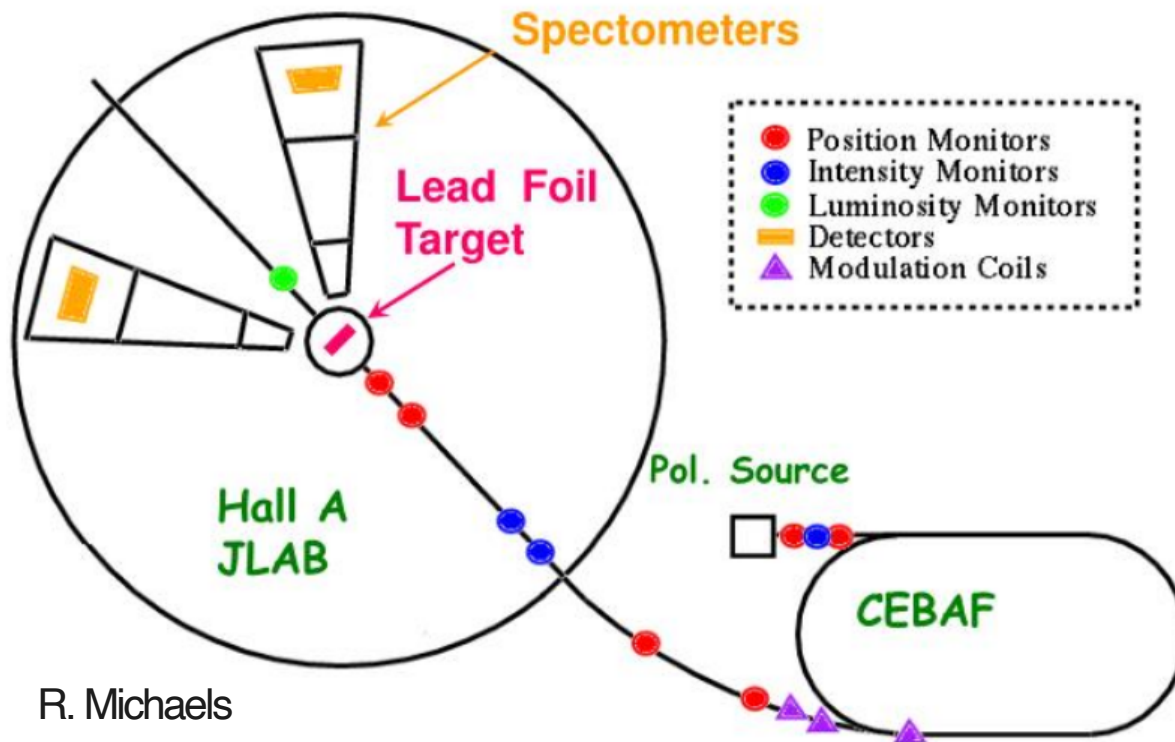
Parity Violating Asymmetry: experiment

Lead and Calcium

Radius Experiments

PREx & CREx @ JLab

$$A_{PV} \sim \frac{G_F}{4\sqrt{2}\pi\alpha} Q^2 \sim 10^{-4} (Q[\text{GeV}])^2$$



→ Spectrometers $\sim 5^\circ$

→ e^- beam $E \sim \text{GeV}$

$$Q_{\text{PREx}}^2 = 0.00616 \text{ GeV}^2$$

$$Q_{\text{CREx}}^2 = 0.0297 \text{ GeV}^2$$

→ Demanding experiment:

For 10^6 electrons or more only **one** of them **interact weakly** with the nucleus

**New experiment on ^{208}Pb @ Mainz !!!
(MREX)**

Parity Violating Asymmetry: theory

To solve the **Dirac equation**

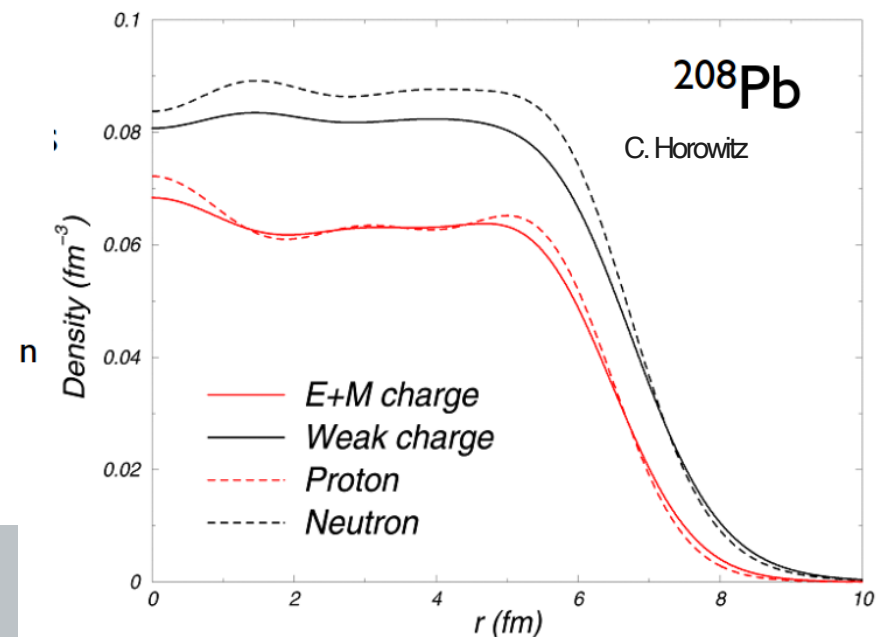
$$\left[\vec{\alpha} \cdot \vec{p} + V_{\text{Coulomb}}(\vec{r}) \pm V_{\text{Weak}}(\vec{r}) \right] \Psi_{\pm} = E \Psi_{\pm}$$

The main inputs are the **electromagnetic** ρ_{ch} and **weak charge** ρ_{W} distributions

$$V_{\text{Coulomb}}(\vec{r}) = Z\alpha \int \frac{\rho_{\text{ch}}(\vec{r}')}{|\vec{r} - \vec{r}'|} d\vec{r}'$$

$$V_{\text{Weak}}(\vec{r}) = \frac{G_F}{2\sqrt{2}} \rho_{\text{W}}(\vec{r})$$

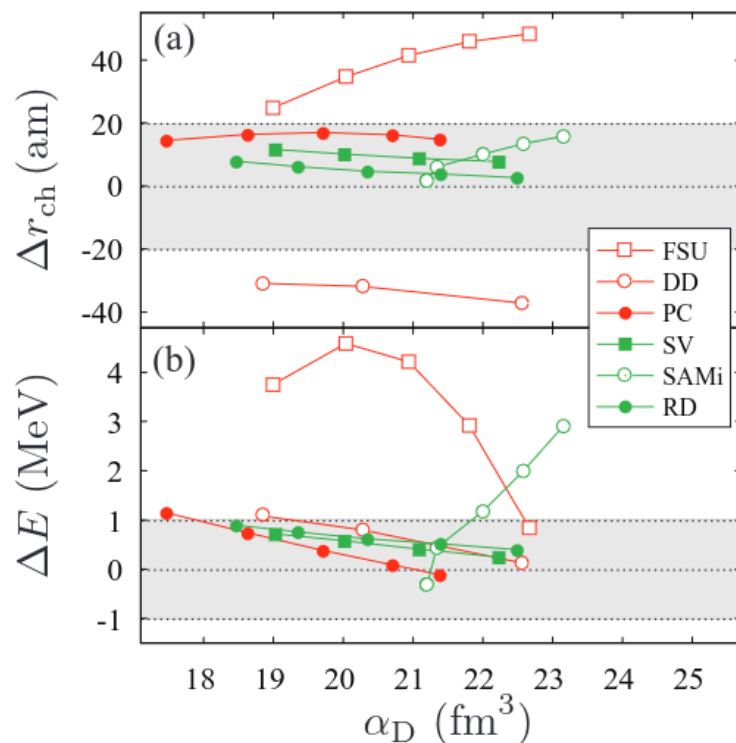
We need to know the **neutron and proton distributions** in nuclei and the **electromagnetic and weak charge form factors** of the **neutron** and the **proton**



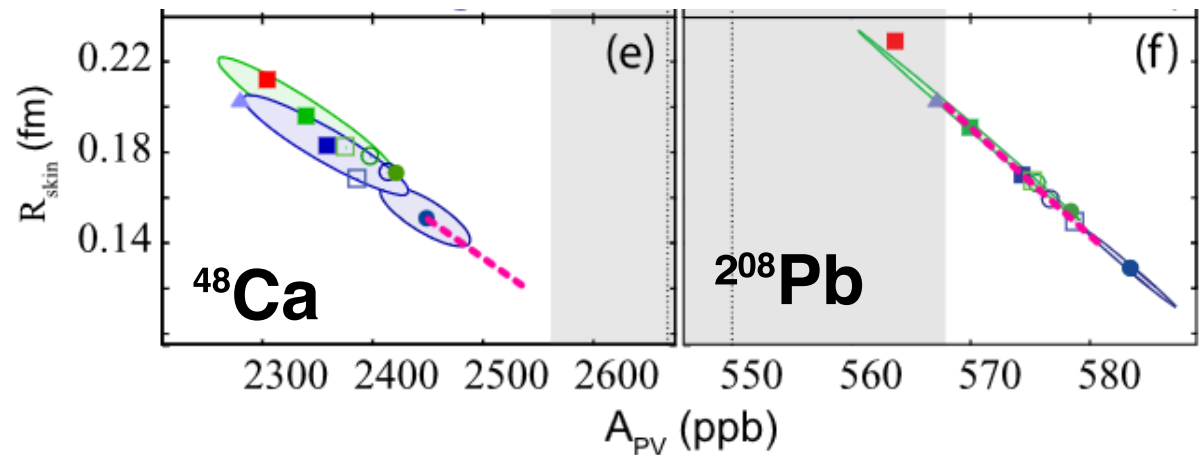
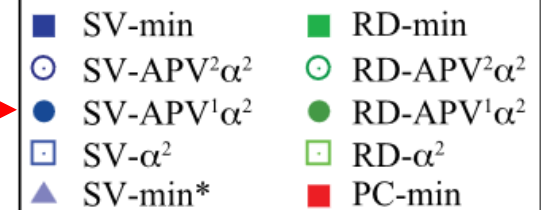
Parity Violating Asymmetry: measurements vs. theory

Selecting those **models** (we consider) **well calibrated to masses and radii**

Theoretical (**EDFs** and **ab initio**) and experimental 1σ errors overlap in ^{208}Pb but not in ^{48}Ca → **No simultaneous description**

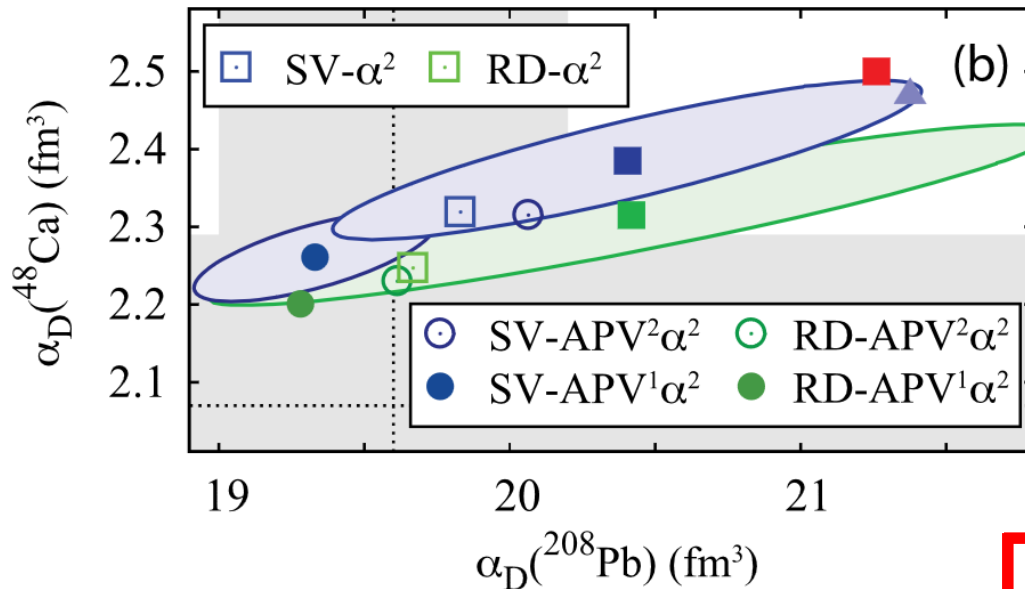


Fitting protocol also including A_{PV} and a_D



Summary: model performance

A_{PV} (sensitive to Δr_{np}) and α_D (sensitive to J and Δr_{np}) in ^{48}Ca and ^{208}Pb



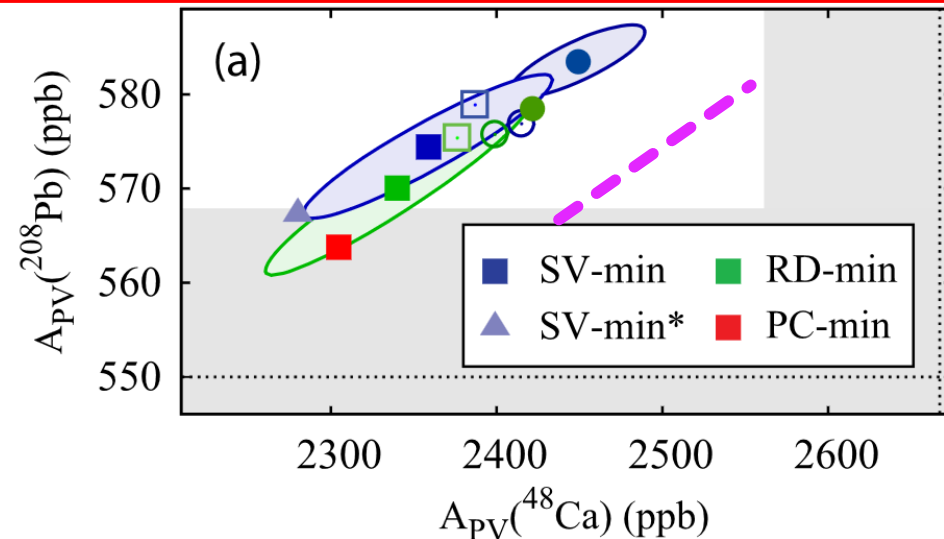
Simultaneous description of dipole polarizabilities → point to a **good understanding of symmetry energy (J) and neutron skins (Δr_{np})**

Ab-initio (B. Hu) Nature Physics (2022)

$$\alpha_D(^{48}\text{Ca}) \quad 2.30^{+0.31}_{-0.26}$$

$$\alpha_D(^{208}\text{Pb}) \quad 22.6^{+2.1}_{-1.8}$$

No simultaneous description of parity violating asymmetries (ground state observable) → point to a **deficient understanding of neutron skins**



Magenta dashed lines from extrapolated Δr_{np} given in G. Hagen et al. Nature Physics 12, 186–190 (2016) and H. Bu et al. Nature Physics (2022)

A_{PV} theoretical corrections?

In all analysis: Coulomb potential has been considered at tree level while Q_{Weak} has been corrected at one-loop level (interference of the γ and Z_0 exchange):

$$[-i\vec{\alpha} \cdot \vec{\nabla} + V_{Coul} \pm V_{Weak}] \Psi_{\pm} = E \Psi_{\pm}$$

First order QED includes: vacuum polarization (VP), self-energy and e^- vertex correction (V-SE) [Jakubassa-Amundsen (2024) JPG: Nucl. Part. Phys. 51 035105]

$$[-i\vec{\alpha} \cdot \vec{\nabla} + V_{Coul} \pm V_{Weak} + V_{VP} + V_{V-SE}] \Psi_{\pm} = E \Psi_{\pm}$$

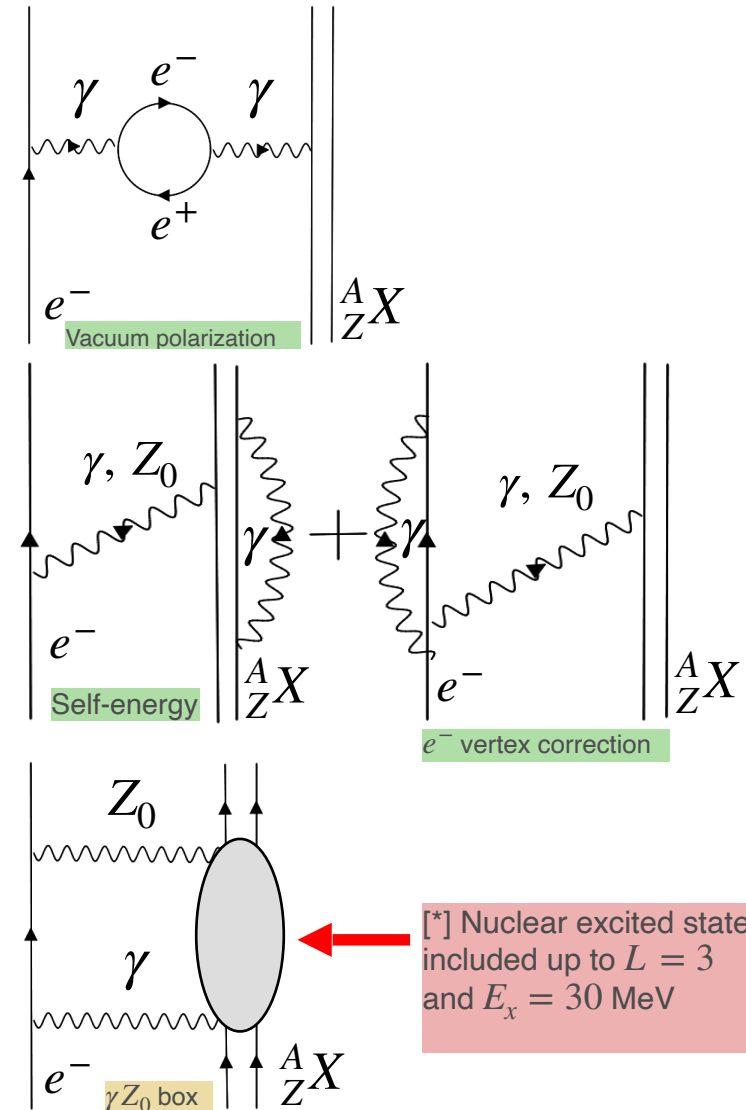
Dispersion corrections: interference of the γ and Z_0 exchange have been shown to be relevant for estimating the Q_{weak} .

On A_{PV} @ PREx kin., corrections **small & cancel**

- Box diagram ~ 0.01 % (reduction)
- QED ~ 0.09 %

[Jakubassa-Amundsen and XRM, PRC 113, 045502 (2026)]

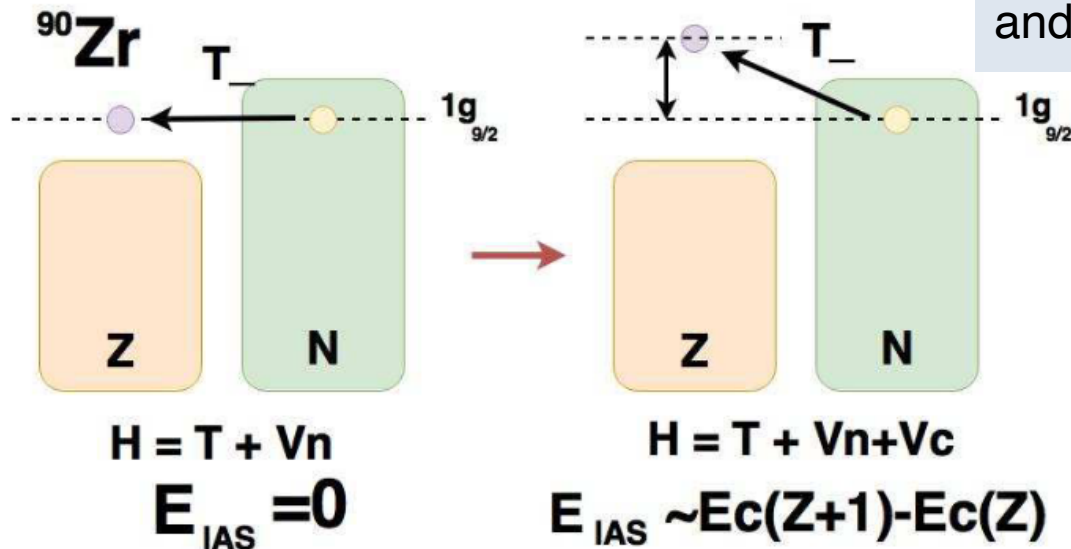
[XRM and Jakubassa-Amundsen PRL 134, 192501 (2025); EPL 154 64001 (2026)]



Isobaric Analog State: Example + theory

$$F = T_{\pm} = \sum_i^A t_{\pm}(i)$$

Charge-exchange experiments



Isospin algebra analogous to spin algebra $s \rightarrow t$ and $\tau \rightarrow \sigma$ (Pauli matrices with $t = \tau/2$)

$$t_- |n\rangle = \frac{1}{2} |p\rangle$$

$$t_+ |p\rangle = -\frac{1}{2} |n\rangle$$

$$T_+^\dagger = T_- \quad T_-^\dagger = T_+$$

$$[T_z, T_{\pm}] = \pm T_{\pm}$$

$$[T_+, T_-] = 2T_z$$

→ non-energy weighted sum rule:

$$\begin{aligned} m_0^- - m_0^+ &= \langle 0 | T_+ T_- | 0 \rangle - \langle 0 | T_- T_+ | 0 \rangle \\ &= \langle 0 | [T_+, T_-] | 0 \rangle = \langle 0 | 2T_z | 0 \rangle \\ &= N - Z \end{aligned}$$

Note: If not isospin-mixing it would be zero!!

→ energy weighted sum rule:

$$m_1 = \sum_{\nu} (E_{\nu} - E_0) |\langle \nu | F | 0 \rangle|^2 = \langle 0 | T_+ [\mathcal{H}, T_-] | 0 \rangle$$

$[\mathcal{H}, T_-] \neq 0$ only if $\mathcal{H}$ contains terms that **breaks isospin invariance**

Isobaric Analog State: Theory

$$F = T_{\pm} = \sum_i^A t_{\pm}(i)$$

→ Hence, the **centroid energy** m_1/m_0 :

$$E_{\text{IAS}} = \frac{\langle 0 | T_+ [\mathcal{H}, T_-] | 0 \rangle}{\langle 0 | T_+ T_- | 0 \rangle} = \frac{1}{N - Z} \langle 0 | T_+ [\mathcal{H}, T_-] | 0 \rangle$$

→ Assuming a simple model: **independent particle** model with only **Coulomb breaking isospin symmetry** (neglect exchange effects)

$$E_{\text{IAS}}^{\text{C,direct}} = \frac{1}{N - Z} \int [\rho_n(\vec{r}) - \rho_p(\vec{r})] U_C^{\text{direct}}(\vec{r}) d\vec{r},$$

$$U_C^{\text{direct}}(\vec{r}) = \int \frac{e^2}{|\vec{r}_1 - \vec{r}|} \rho_{\text{ch}}(\vec{r}_1) d\vec{r}_1$$

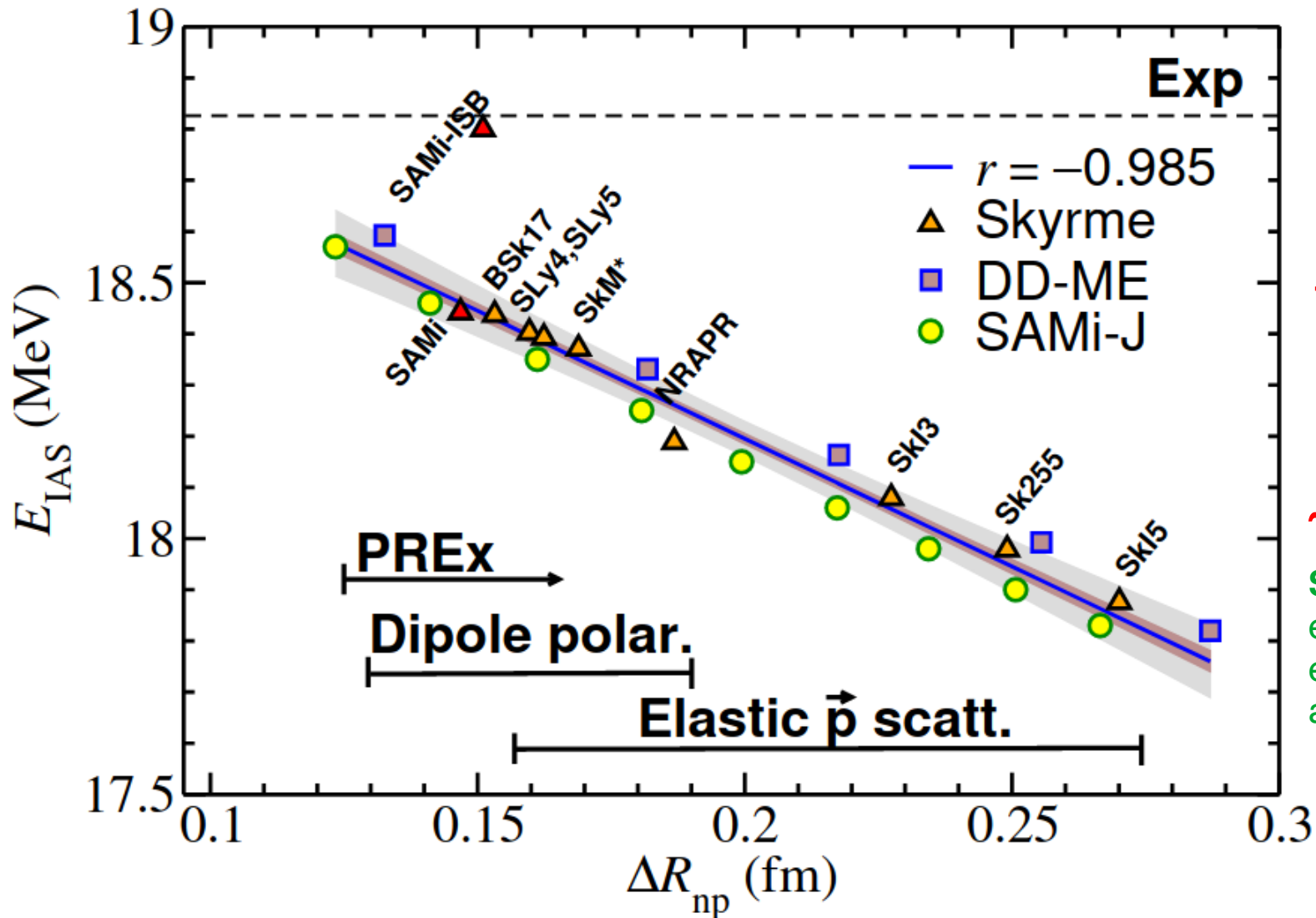
→ Assuming sharp sphere to describe ρ_n and ρ_p and $\rho_{\text{ch}} = \rho_p$

$$U_C^{\text{direct}}(\vec{r}) = \begin{cases} \frac{Ze^2}{2R_p} \left(3 - \frac{r^2}{R_p^2} \right) & \text{for } r < R_p \\ \frac{Ze^2}{r} & \text{for } r > R_p \end{cases}$$

$$\begin{aligned} E_{\text{IAS}} &\approx E_{\text{IAS}}^{\text{C,direct}} \\ &\approx \frac{6}{5} \frac{Ze^2}{R_p} \left(1 - \frac{1}{2} \frac{N}{N - Z} \frac{R_n - R_p}{R_p} \right) \\ &\approx \frac{6}{5} \frac{Ze^2}{r_0 A^{1/3}} \left(1 - \sqrt{\frac{5}{12}} \frac{N}{N - Z} \frac{\Delta R_{\text{np}}}{r_0 A^{1/3}} \right) \end{aligned}$$

Isobaric Analog State:

Theory+experiment



Exp errors in IAS ~
tens of keV

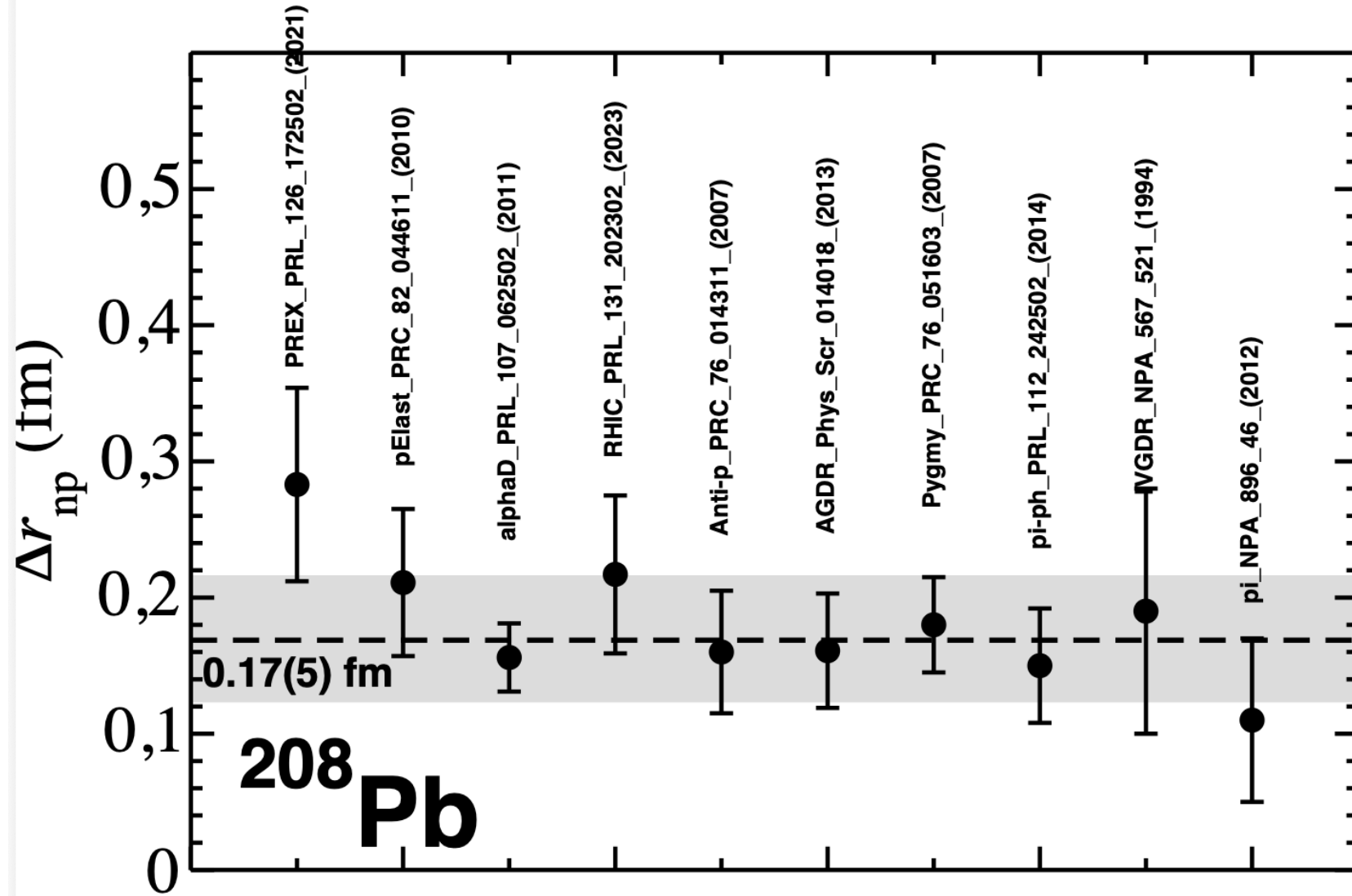
(or smaller)

Exp width IAS

~ hundreds of keV

SAMI-IB: includes ISB
effects due to Coulomb
exchange, QED corrections
and nuclear ISB

Summary on Δr_{np} in ^{208}Pb :



Summary



Different ways to learn about the **neutron distribution** in atomic nuclei using **different observables** provide **different answers**

However, within **1.5–2 σ** **all looks fine**, both from phenomenologic **Energy Density Functionals** and from **Ab Initio**

From Theory:

- An effort to better understand the **parity violating asymmetry** and the **beam normal spin asymmetry**^[*] in **^{208}Pb** is needed [PREX & CREX, PRL 128, 142501 (2022)].
- An effort to better understand the **systematics** on the **dipole polarizability** would be of interest [see e.g. Sn chain in Bassauer et al. PLB 810, 135804 (2020)].
- An effort to **understand ISB effects in the medium** from first principles [see e.g. Sagawa et al. Phys. Rev. C 109, L011302 (2024)]

From Experiment (low-energy):

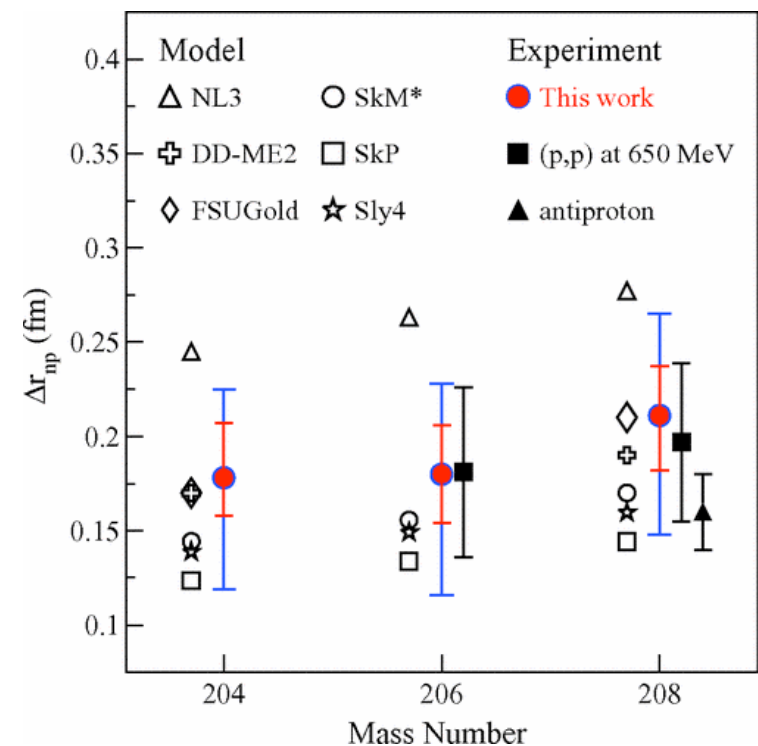
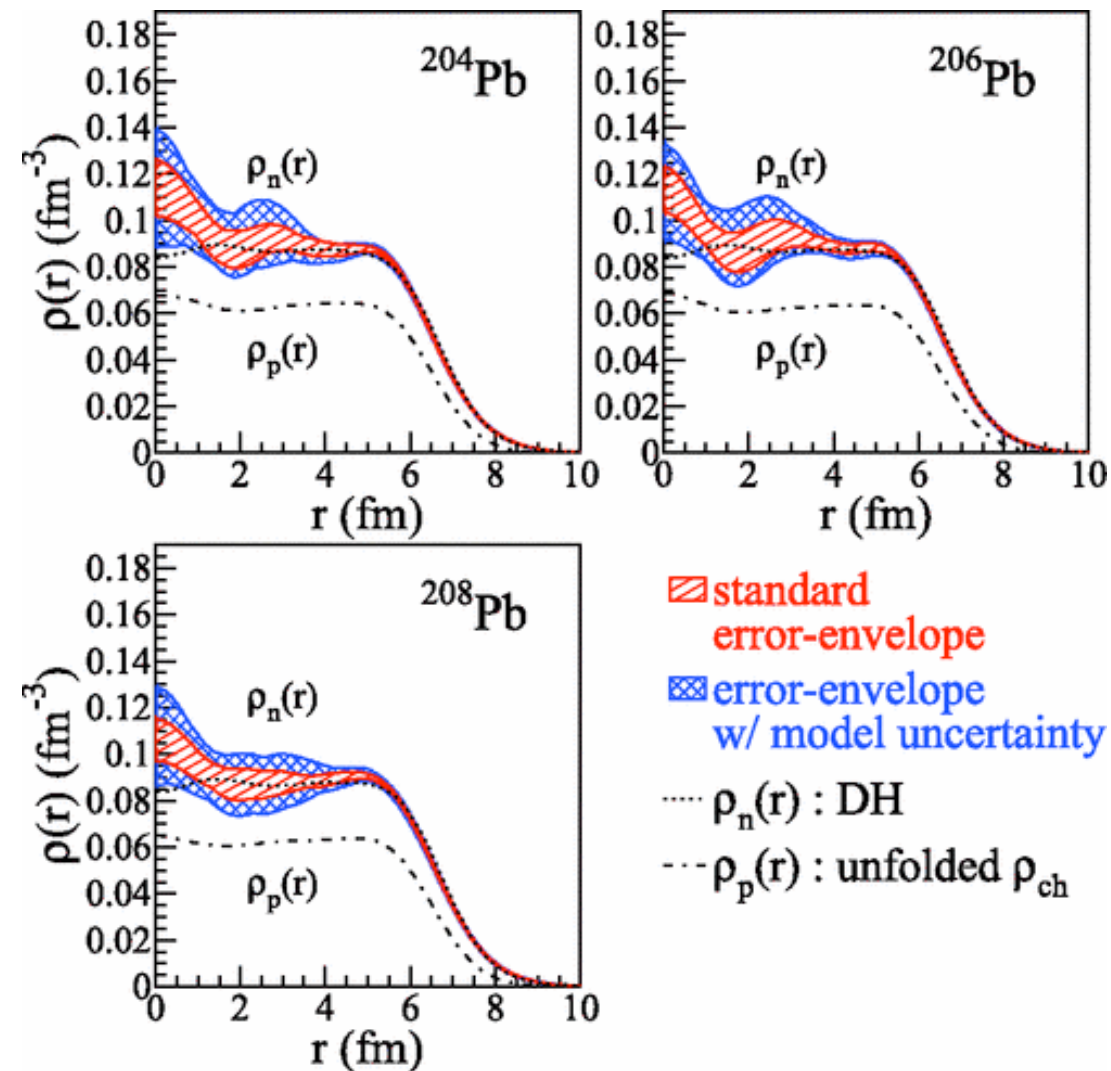
- An effort to improve the accuracy in the **parity violating asymmetry in ^{208}Pb** (and measure **other Q values**) **is needed**. Measuring other nuclei would also be desirable.
- **Systematic** measurements of the **dipole polarizability** along **neutron rich** isotopic chains (e.g. $N > 74$ Sn isotopes) could help testing models and improve our understanding of this observable.

Collaborators

- Gianluca **Colò** (University of Milan)
- Pietro **Klausner** (University of Milan)
- Tomoya **Naito** (University of Tokyo)
- Xavier **Vinyes** & Mario **Centelles** (University of Barcelona)
- Jorge **Piekarewicz** (Florida State University)
- Nils **Paar** & Dario **Vretenar** (University of Zagreb)
- Bijay K. **Agrawal** (Saha Institute of Nuclear Physics)
- P.-G. **Reinhard** (University of Erlangen-Nürnberg)
- Witold **Nazarewicz** (FRIB and Michigan State University)
- Doris H. **Jakubassa-Amunsden** (Ludwig-Maximilians-Universität München)

RCNP - proton elastic scattering

Polarized **proton** elastic scattering @ 295MeV
sensitive to the overall **strong size** of the nucleus



Neutron density distributions of $^{204,206,208}\text{Pb}$ deduced via proton elastic scattering at $E_p = 295$ MeV

J. Zenhiro^{1,2}, H. Sakaguchi^{1,2}, T. Murakami¹, M. Yosoi^{1,2}, Y. Yasuda^{1,2}, S. Terashima^{1,2}, Y. Iwao¹, H. Takeda², M. Itoh^{3,4} et al.

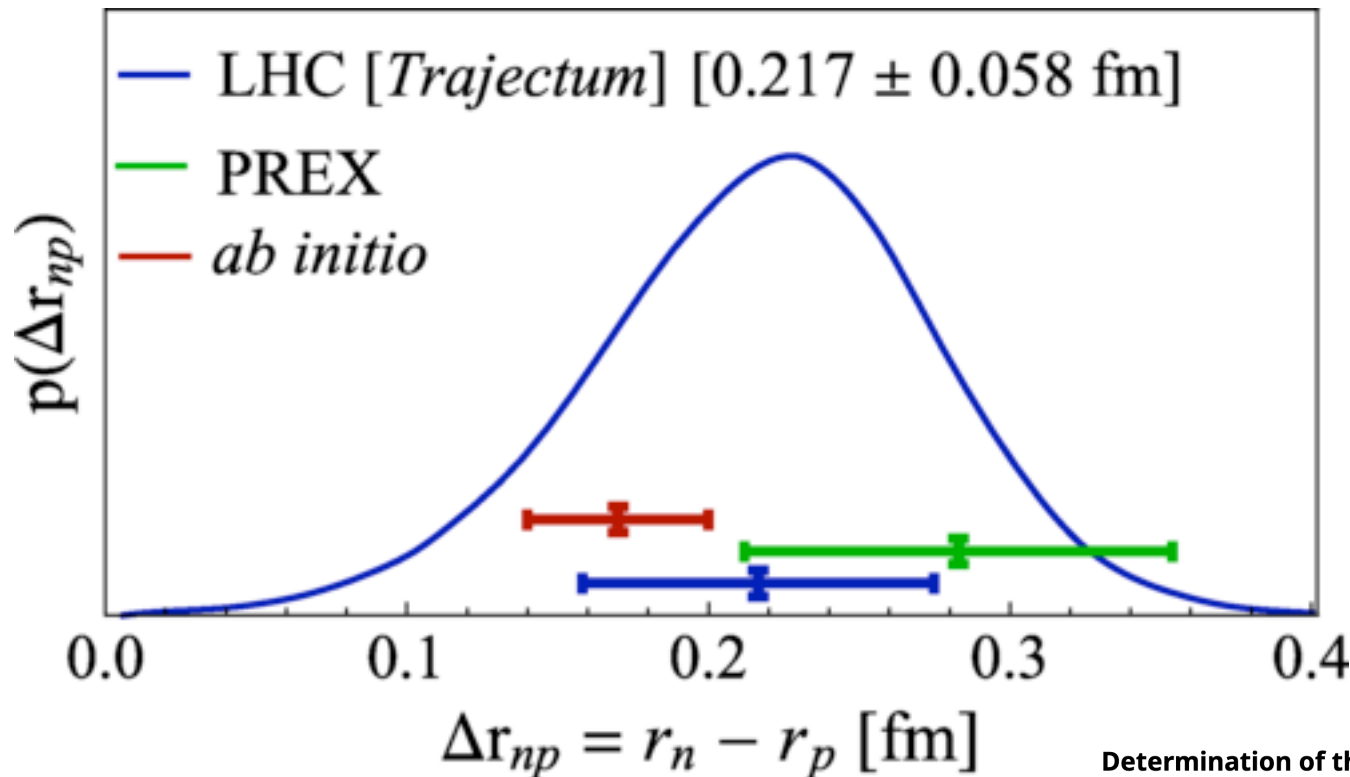
Show more

Phys. Rev. C 82, 044611 - Published 22 October, 2010

$$\Delta r_{\text{np}} = 0.211^{+0.054}_{-0.063} \text{ fm}$$

LHC - Relativistic Heavy Ion Collisions

Particle distributions and **collective flow** in 208Pb + 208Pb
RHIC @ LHC are **sensitive** to the overall strong **size** of the
nuclei involved.



Determination of the Neutron Skin of ^{208}Pb from
Ultrarelativistic Nuclear Collisions

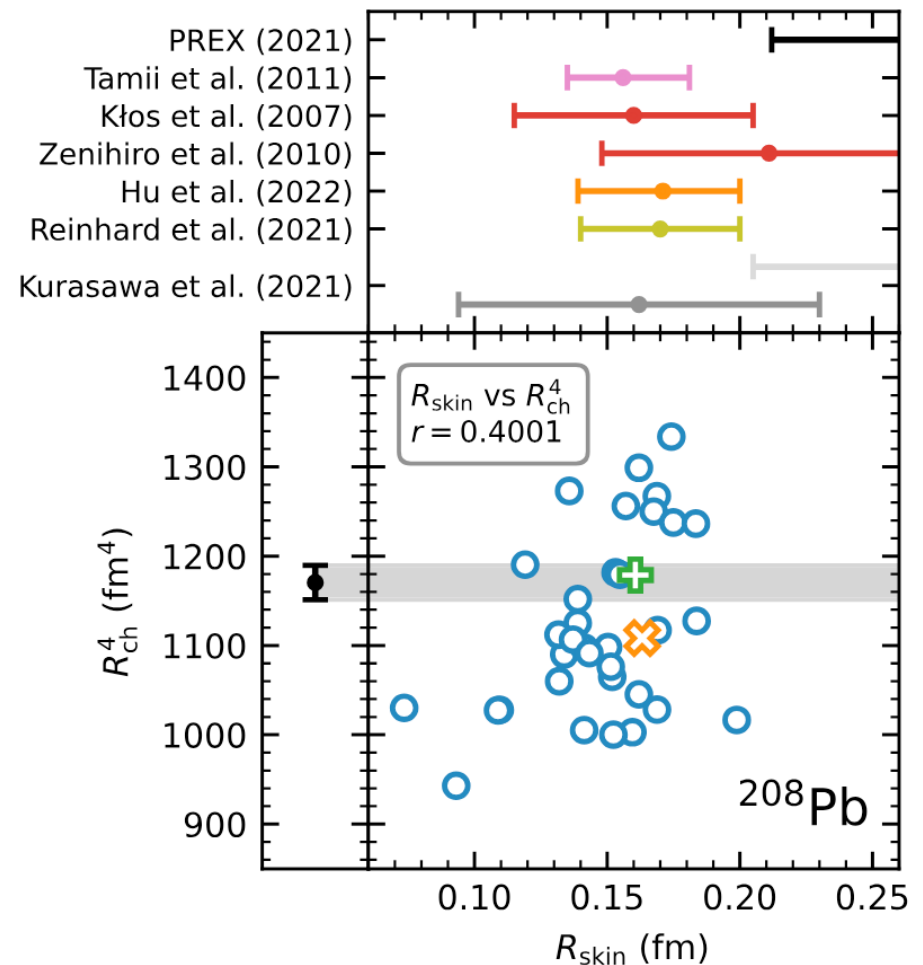
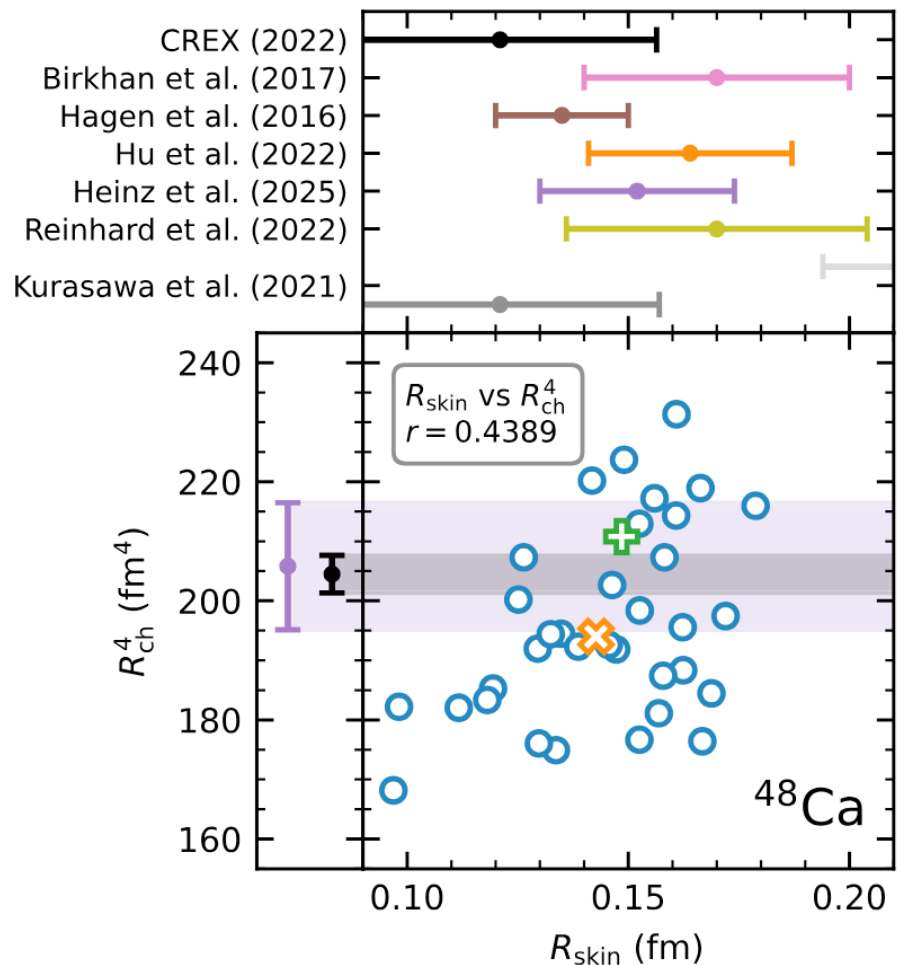
Giuliano Giacalone¹, Govert Nijss², and Wilke van der Schee^{3,4}

Show more

Phys. Rev. Lett. 131, 202302 – Published 15 November, 2023

$$\Delta r_{np} = 0.217 \pm 0.058 \text{ fm}$$

Summary on Δr_{np} in ^{48}Ca and ^{208}Pb



R_{ch}^4 inferred from expt. R_{ch}^2
 R_{ch}^4 inferred from theor. R_{ch}^2

$\Delta\text{NNLO}_{\text{GO}}$
 1.8/2.0 (EM7.5)

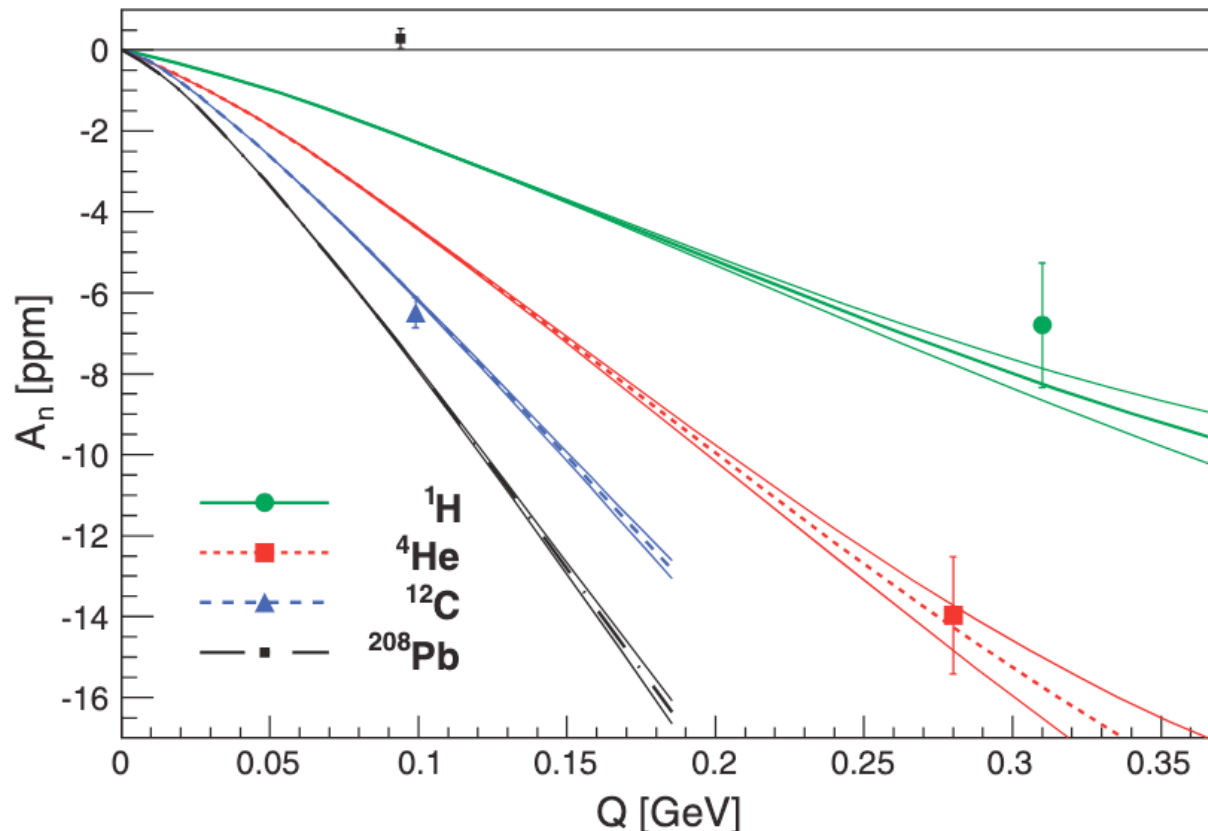
Nonimplausible Hamiltonians

Ab initio computations of the fourth-order charge density moments of ^{48}Ca and ^{208}Pb

T. Miyagi^a, M. Heinz^{b,c}, A. Schwenk^{d,e,f}

Beam normal spin asymmetry (A_n) (aka Alayzing power or Sherman function)

Is the asymmetry in the scattering cross section when the incident electron beam is polarized perpendicular (longitudinal $\rightarrow A_{pv}$) to the scattering plane



$\Rightarrow$ Important to understand A_{pv} since it represents a potentially large systematic correction to measured asymmetries.

In Born approximation (one-photon exchange), $A_n = 0$ because time-reversal symmetry forbids such an asymmetry.

Arises from interference between one-photon exchange and the absorptive part of two-photon exchange amplitudes.

New Measurements of the Transverse Beam Asymmetry for Elastic Electron Scattering from Selected Nuclei

S. Abrahamyan⁴⁵, A. Acha¹⁰, A. Afanasev¹¹, Z. Ahmed³³, H. Albataineh⁶, K. Aniol³, D. S. Armstrong⁷, W. Armstrong³⁵, J. Arrington¹ et al. (HAPPEX and PREX Collaborations)

Show more

Phys. Rev. Lett. **109**, 192501 – Published 5 November, 2012
DOI: <https://doi.org/10.1103/PhysRevLett.109.192501>

New Measurements of the Beam-Normal Single Spin Asymmetry in Elastic Electron Scattering over a Range of Spin-0 Nuclei

D. Adhikari¹, H. Albataineh², D. Androic³, K. Aniol⁴, D. S. Armstrong⁵, T. Averett⁵, C. Ayerbe Gayoso⁵, S. Barcus⁶, V. Bellini⁷ et al. (PREX and CREX Collaborations)

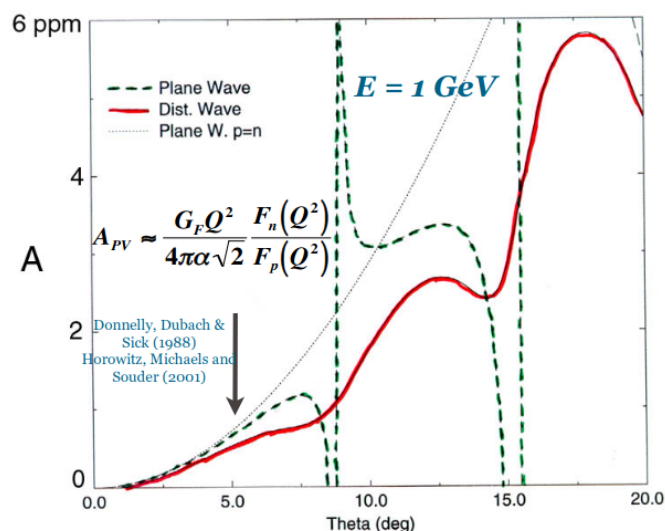
Show more

Phys. Rev. Lett. **128**, 142501 – Published 8 April, 2022
DOI: <https://doi.org/10.1103/PhysRevLett.128.142501>

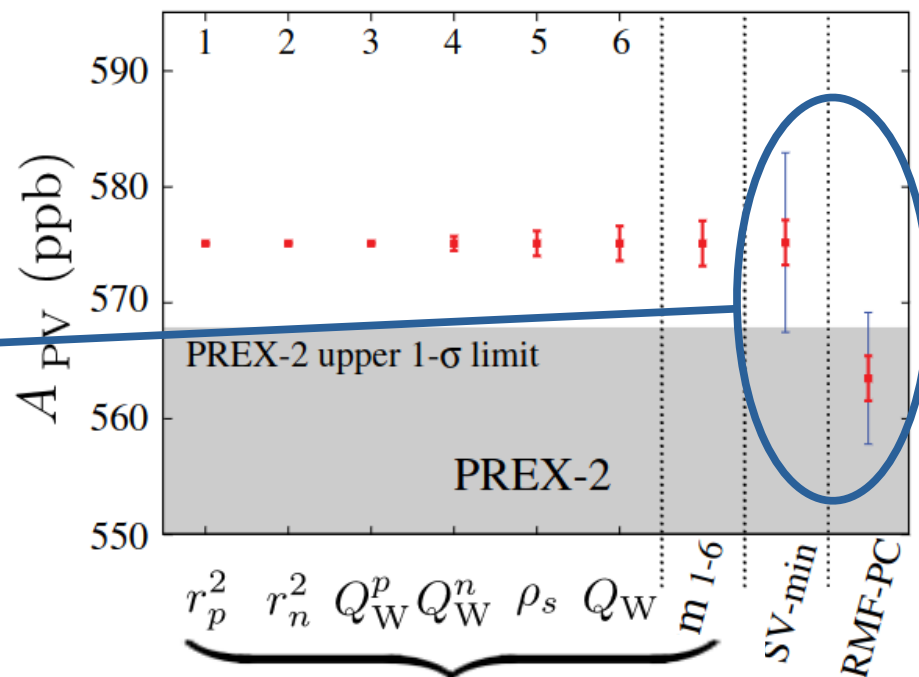
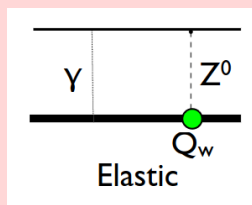
Parity Violating Asimmetry: theory

The **main uncertainties** come from **nuclear model errors** on the description of the **neutron distribution (blue error bars)**

→ **Coulomb distortions** are important (order αZ)



Are γZ_0 box corrections important? not included



Hadronic uncertainties less relevant

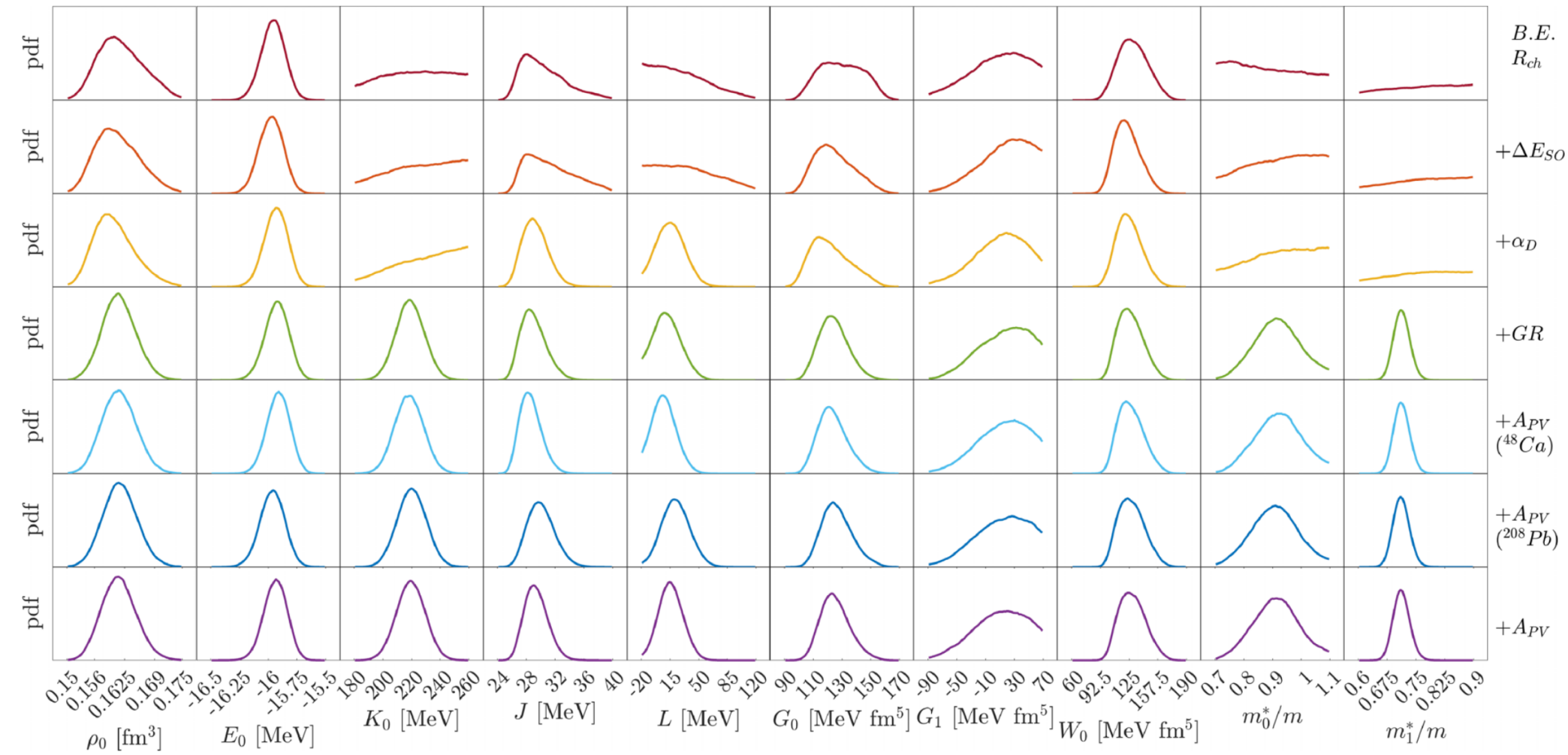
Parameter	Value
$\langle r_p^2 \rangle$ (fm ²)	0.726 ± 0.019
$\langle r_n^2 \rangle$ (fm ²)	-0.1161 ± 0.0022
μ_p	$2.792\,847$
μ_n	-1.9130
$Q_p^{(W)}$	0.0713 ± 0.0001
$Q_n^{(W)}$	-0.9888 ± 0.0011
ρ_s	-0.24 ± 0.70
κ_s	-0.017 ± 0.004
$Q_{126,82}^{(W)}$	-117.9 ± 0.3

Information Content of the Parity-Violating Asymmetry in ^{208}Pb

Paul-Gerhard Reinhard, Xavier Roca-Maza, and Witold Nazarewicz
Phys. Rev. Lett. **127**, 232501 – Published 29 November 2021

Bayesian inference Skyrme EDF: can we accommodate α_D and A_{PV} without compromising other observables?

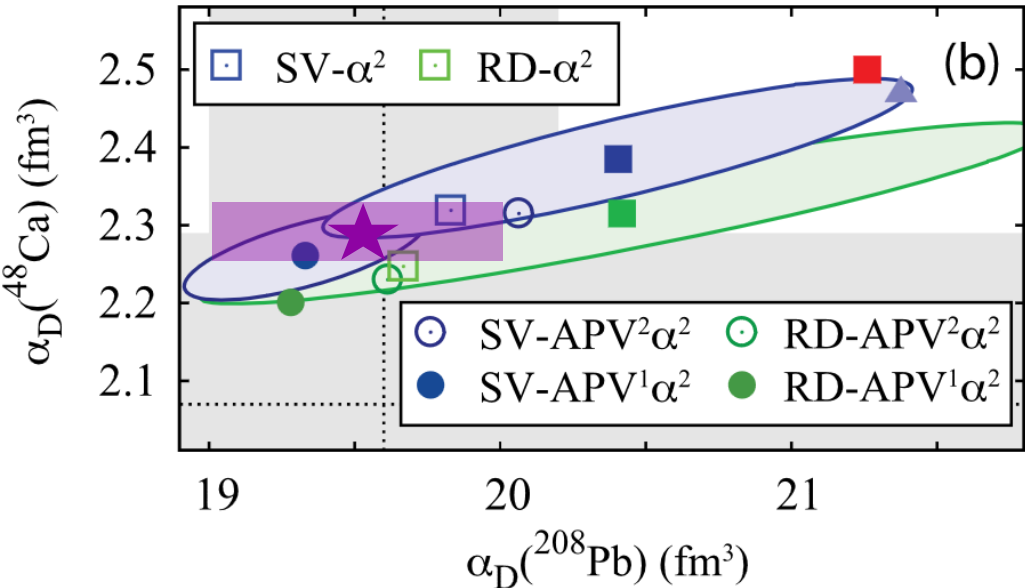
By P. Klausner



Bayesian inference Skyrme EDF: can we accommodate α_D and A_{PV} without compromising other observables?

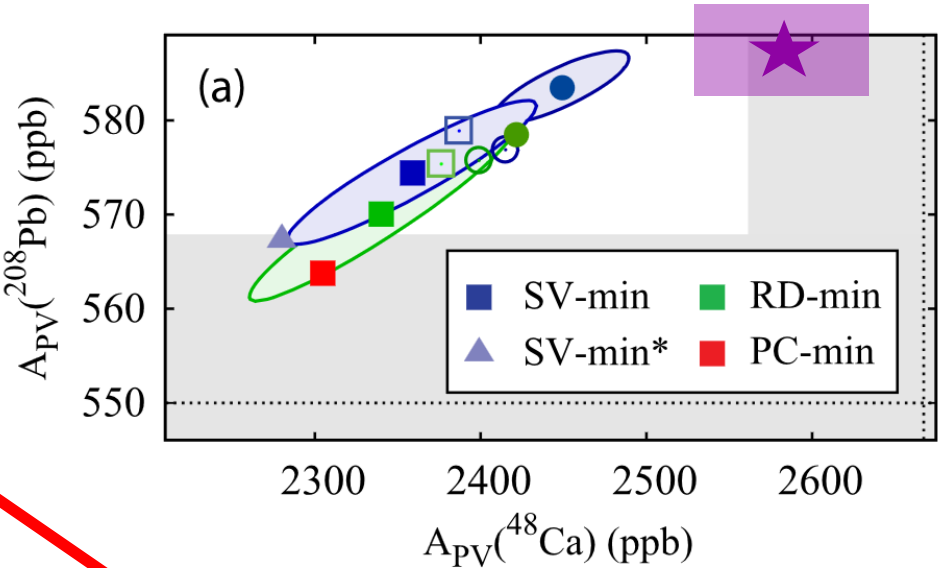
Pietro Klausner, Gianluca Colò, Xavier Roca-Maza, and Enrico Vigezzi
 Phys. Rev. C 111 014311 (2025)

By P. Klausner 



	B.E. (MeV)	R_{ch} (fm)	ΔE_{So} (MeV)
^{208}Pb	1636 ± 1.8	5.49 ± 0.03	2.34 ± 0.16
^{48}Ca	417 ± 1.2	3.51 ± 0.02	1.92 ± 0.20
^{40}Ca	342 ± 1.6	3.50 ± 0.02	—
^{56}Ni	482 ± 1.4	—	—
^{68}Ni	590 ± 1.0	—	—
^{100}Sn	826 ± 1.6	—	—
^{132}Sn	1103 ± 1.7	4.71 ± 0.03	—
^{90}Zr	784 ± 1.3	4.27 ± 0.02	—
Isoscalar resonances			
	$E_{\text{GMR}}^{\text{IS}}$ (MeV)	$E_{\text{GQR}}^{\text{IS}}$ (MeV)	
^{208}Pb	13.5 ± 0.3	10.8 ± 0.4	
^{90}Zr	17.8 ± 0.4	—	

	α_D (fm ³)	$m(1)$ (MeV fm ²)	A_{PV} (ppb)
^{208}Pb	19.5 ± 0.5	958 ± 22	589 ± 5
^{48}Ca	2.30 ± 0.08	—	2591 ± 54



Keeping ground and excited state properties within typical Skyrme-EDF accuracy